Gv How Know if a rarional no: 1, P, g EI, 2 = 0 18 repeating or Terminating without dividing RepeatingX Ex: 29 Pechaan 25 2º.52 is of the form 2x5" Ex: 37 where mineW. 2×3-13 Ex: 91 (pritory $\Rightarrow \frac{.91}{.44} = \frac{13}{2} = 6.5 \text{ }$ mmating KAAM KI BAAT : Every Integer 12 a Ra Number B'wz : 2 = 2 form P, 2EI, 2=0. 0=0 IRRATIONAL NO: 8 Neither Repeating nor Terminating Decimals. Ex: J= +414 -vision By J3= 1.73205-5 = 2.236 - -O is not defined e ~ 2.718 - - -In Mathematics T ~ 3.14 ----





Let P(x) be a polynomial of degree ≥ 1 and 'a' is any real number. If P(x) is divided by (x - a), then the remainder is P(a).

$P(x) = x^{2} - 3x^{2} + 3x + 5$ $x^{2} - 2x + 1 Quotient$ $x - 1 x^{2} - 3x^{2} + 3x + 5$ $divisor \frac{x^{2} - x^{2}}{-2x^{2} + 3x}$ $-\frac{2x^{2} + 3x}{-2x^{2} + 3x}$ $\frac{-2x^{2} + 3x}{-2x^{2} + 3x}$ $\frac{-2x^{2} + 3x}{-2x^{2} + 3x}$ $\frac{-2x^{2} + 3x}{-2x^{2} + 3x}$		- 3x2+3x+5. hendivided by X-1
$\frac{1}{2} \frac{1}{3} \frac{1}$		x=0 $f = (-1) \cdot 1 + 6 = 5$ $f = (-1) \cdot 1 + 6 = 5$
т	Divisor	Remainder
X-a=0 P(x)	X-a	P (a)
(x=g)	X+Q	P(-a)
2x+3=0 $x+a=0x=-3 _{2} (x=-a)$	2×+3	P(-3/2)
	3X-2	P(5 3)

Remark

- i. p(-a) is remainder on dividing p(x) by (x + a)
- ii. $p\left(\frac{b}{a}\right)$ is remainder on dividing p(x) by (ax b)
- iii. $p\left(\frac{-b}{a}\right)$ is remainder on dividing p(x) by (ax + b)
- iv. $p\left(\frac{b}{a}\right)$ is remainder on dividing p(x) by (b ax)

$$[\because \mathbf{x} + \mathbf{a} = \mathbf{0} \Rightarrow \mathbf{x} = -\mathbf{a}]$$
$$[\because \mathbf{a}\mathbf{x} - \mathbf{b} = \mathbf{0} \Rightarrow \mathbf{x} = \frac{\mathbf{b}}{\mathbf{a}}]$$
$$[\because \mathbf{a}\mathbf{x} + \mathbf{b} = \mathbf{0} \Rightarrow \mathbf{x} = -\frac{\mathbf{b}}{\mathbf{a}}]$$
$$[\because \mathbf{b} - \mathbf{a}\mathbf{x} = \mathbf{0} \Rightarrow \mathbf{x} = \frac{\mathbf{b}}{\mathbf{a}}]$$

FACTOR THM.
Remainder in Disguise. Theorem.
Let P(x) be a poly of degree > 1 & if
$f(\alpha) = 0 \implies x - \alpha \text{ is } \alpha \text{ factor of } P(x) $
Conversely if (x-a) is factor of P(x) then P(a)=0.

Name of Exponent Rules	Rule		
Zero Exponent Rule	$a^0 = 1$ (Where $a \neq 0$)		
Identity Exponent Rule	$a^1 = a$		
Product Rule	$a^m \times a^n = a^{m+n}$		
Quotient Rule	$a^m/a^n = a^{m-n}$		
Negative Exponents Rule	$a^{-m} = 1/a^m; (a/b)^{-m} = (b/a)^m$		
Power of a Power Rule	$(a^m)^n = a^{mn}$		
Power of a Product Rule	$(ab)^m = a^m b^m, (a^p b^q)^\alpha = a^{p\alpha} b^{q\alpha}$		
Power of a Quotient Rule	$(a/b)^m = a^m/b^m$		
Fractional Rule	$(a/b)^{m} = a^{m}/b^{m}$ $a^{1/n} = \sqrt[n]{a}; a^{m/n} = (a^{m})^{1/n} = \sqrt[n]{a^{m}} = (a^{1/n})^{m} = (\sqrt[n]{a})^{m}$		

An Important Result

a + 6	+c=ab-bc-ca 30 +a	, 6, C F R
	ality holds ie	
****	$a^3+b^2+c^2-ab-bc-ca=0$ H $a=b=c$	***

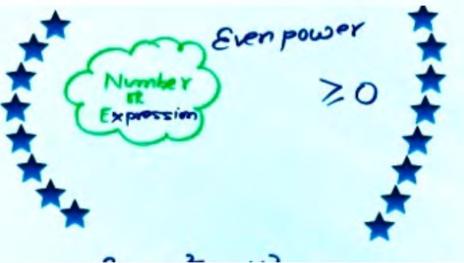
An Important Result

★ If x, y ∈ R & $x^2 + y^2 = 0 \implies x = 0 \implies y = 0$

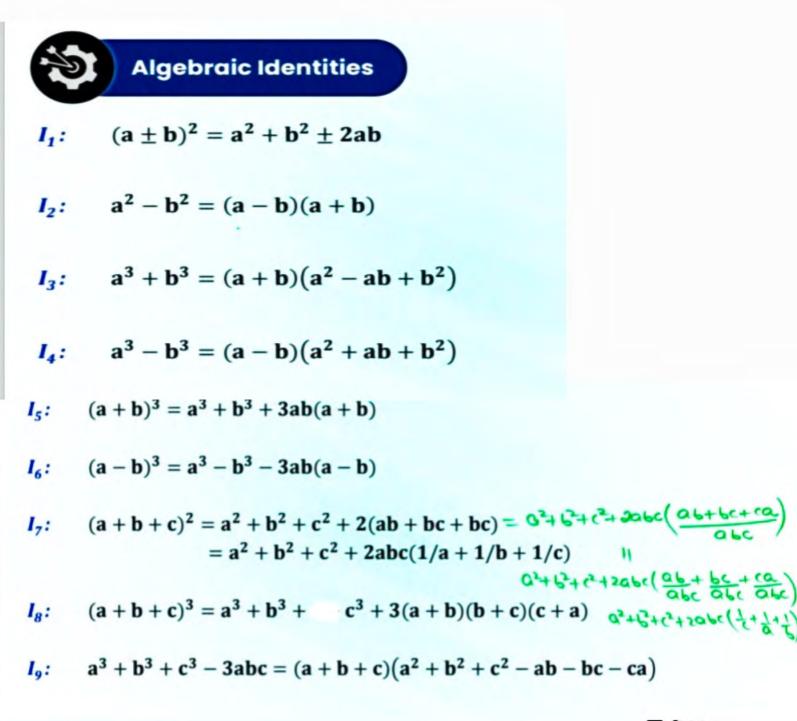
Generalization:

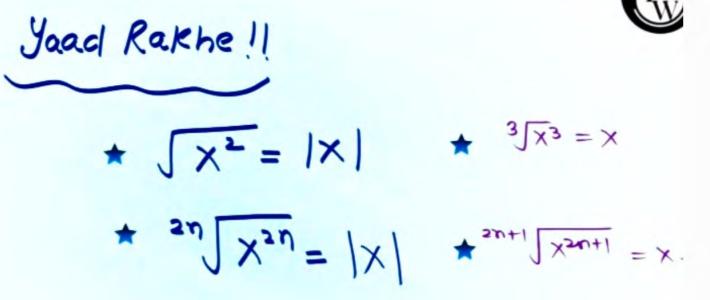
If $a_1 a_2 \dots a_n \in R$ then $a_1^2 + a_2^2 + \dots + a_n^2 = 0$ then $a_1 = a_2 = \dots = a_n = 0$

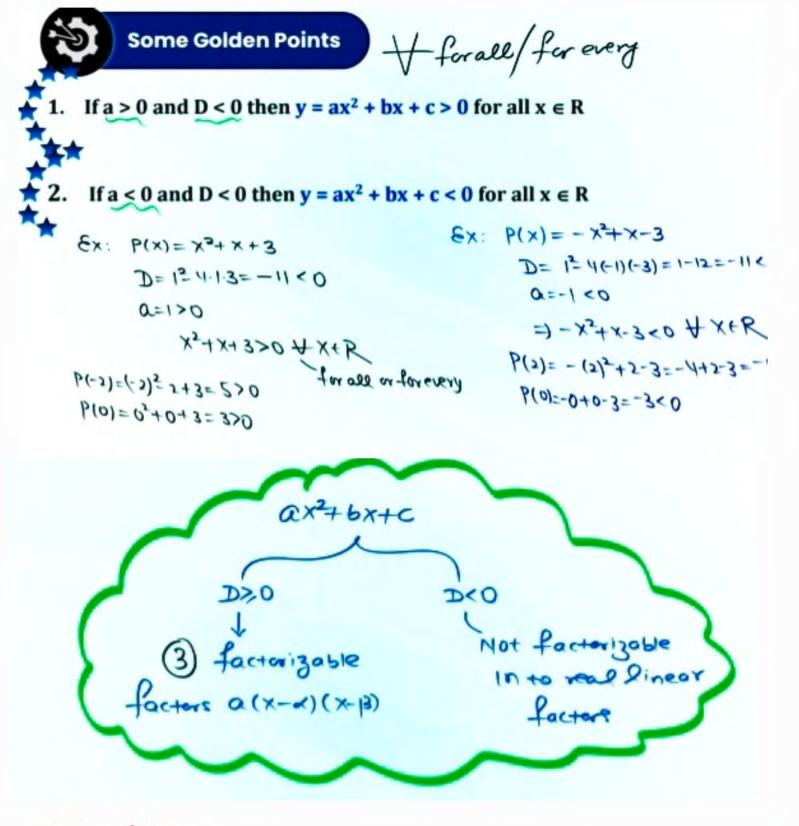
Ex: find x sy
$$4x^{2}+4x+1+y^{2}-6y+9=0$$
, x, y f R
 $(2x)^{2}+2\cdot 2x\cdot 1+1^{2}+y^{2}-2\cdot 3\cdot y+3^{2}=0$
 $(2x+1)^{2}+(y-3)^{2}=0$
 $2x+1=0 = y -3=0$
 $x=-y_{2} = y = 3$.



(Any positive real number) Any real power







Inequalities

- B1: We can add (or subtract) any number 'k' on both sides of inequality. Doing this will not change the sign of inequality.
- B2: We can multiply (or divide) any non-zero number 'k' on both sides of inequality and sign of inequality will change according to sign of 'k' that is
 - If k > 0 then sign of inequality will remains same,
 - If k < 0 then sign of inequality will get reversed.</p>

- B3 :Squaring (raising even power both side) is only allowed when both sides
of inequality are non negative.3>23>23>23>23>23>23>23>33>3
- B4: Raising both sides to odd power is fine. $\underbrace{\text{Ex: } 372}_{\text{272}} \text{$6x:-27-3$}_{\text{272}} \text{$6x:-27-3$}_{\text{$272$$

 $\begin{cases} x: 5>-2 \\ us>-8 \\ us>-8 \\ di>-3/8 \\ di>-3/$

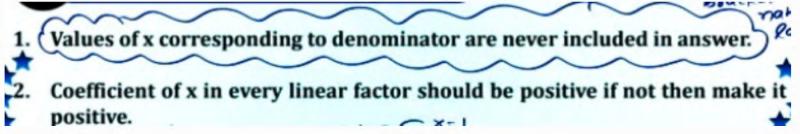
Inequalities can be multiplied provided both sides are positive and have same sign of inequality, but they can not be divided.

Method of Intervals

Steps Involved

- 1. Make one side of inequality 0.
- 2. Factorize the non zero side in to linear factors 🛫
- 3. Put each linear factor equal to zero & find value of x.
- 4. Plot all values of x on a number line.
- Start with a positive sign on the extreme right part & then place negative, positive signs alternately.

Important Point to Note



G

Ex: 5>-2) Ex: 3>-7)SBS 2574)SBS 9749X

Case of Repeated Factors

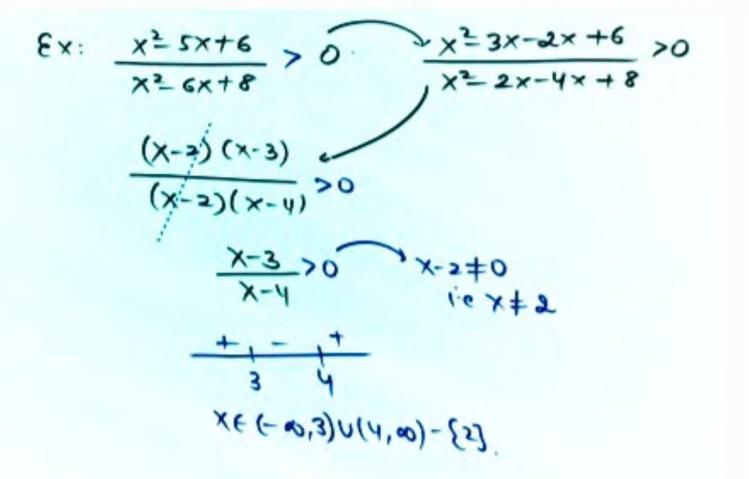


B₁: Every odd integral power of a linear factor is treated as 1.

: In case of even power of any factor, first we assume that it is always positive. So we delete it from the inequality but in the end we make a direct check at that value of x where the deleted factor is zero.

In case if a factor is eliminated

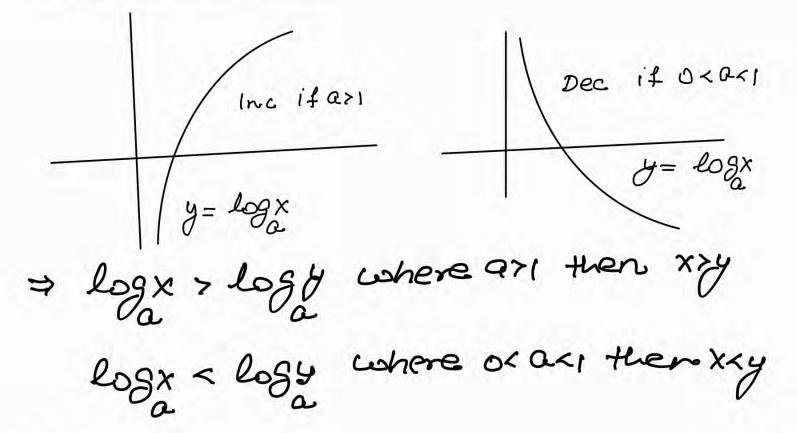
In this case the factor that is cancelled in the Numerator & Denominator, it is put not equal tozero & it's roots are never included in answer



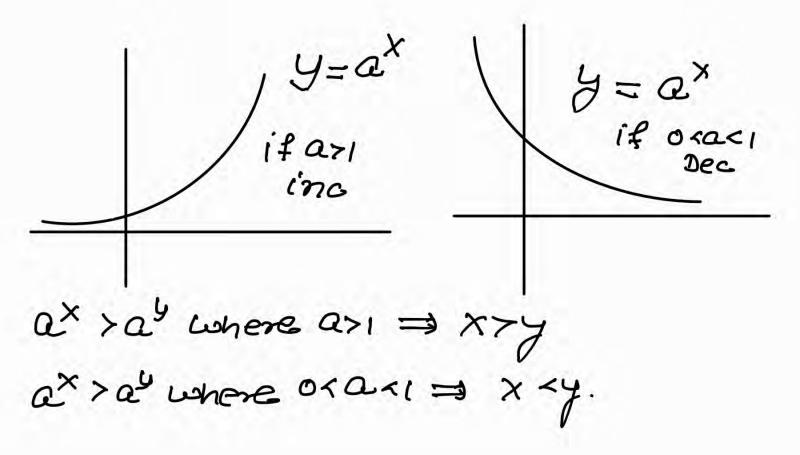
whenever an equ * 5/2=1×1 1* consists of two or *TX+ 1 > A , XER+ more variables try to * |Y|= (x, xx0) make perfect squares *]x+ 1 <- 2, x ER *> 027,0,0 ER the for In an inequality we can add or subtract any no. From both * IFanazz-somer then =100g +> If we multiply or divide both $a_1^2 + b_2^2 + \dots + a_n^2 = 0$ then <ides by any mat. the no: sign $a_1 = a_2 = \cdots = a_n = 0$ of inequality remains same * coeff of xin each linear to the multiply or divide both sides by any -ve no: sign factor should the of inequality reversed * ax2+bx+c * a=1 (a= 0) 0°-+rot-define +> if D: (0, a 70 + ax2+bx+c70 +xER * 574 (2) 25716 iF plo, aco Agar dono sides non-the - axetbx+c co +xER 2 +> DTO then quad is factorizable ho then we can square 7 into real linear Factors 2 $*(3-x)^{2}=(x-3)^{2}$ $ax^{2} + bx + c = a(x - a)(x - b)$ but (4-x) = (x-4)3 x, B= - b= J b=-49 + log N denotes power to which * $\log_a b = \frac{\log_a b}{\log_a a}$ should be raised in order to *logob = togba get * logan is defined if aro, a=1, N70 * $\alpha^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = 1, \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = -1, \log_a^a = -1 \\ \int_a^{\log_a N} = N_1 \log_a^a = -$ * log av mx = x loy m * logal = 0 * log 1 is not defined oz it can not give definite value + lag az . log az log ay --Jaj Jaz Jaz $t \log_a(m,n) = \log_a(m) + \log_a(n)$ (=- log an = log an. Jani) Jai * loga (m) = loga(m) - loga(n) * 10gam2 = X-10gam

Scanned with CamScanner

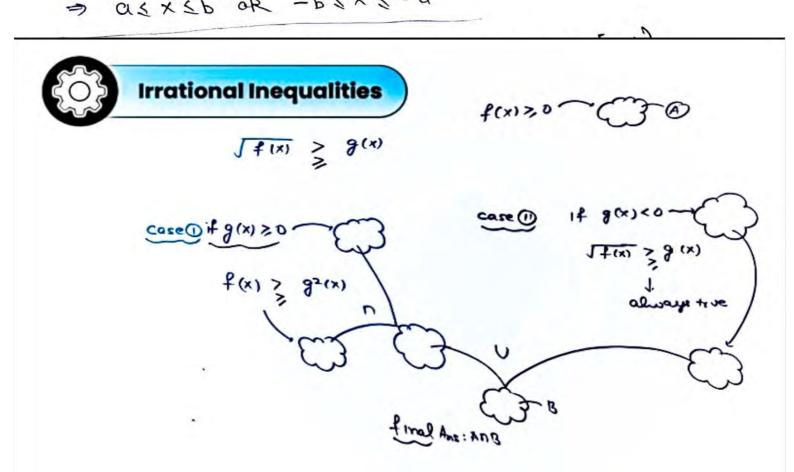
Logarithmic Inequalities

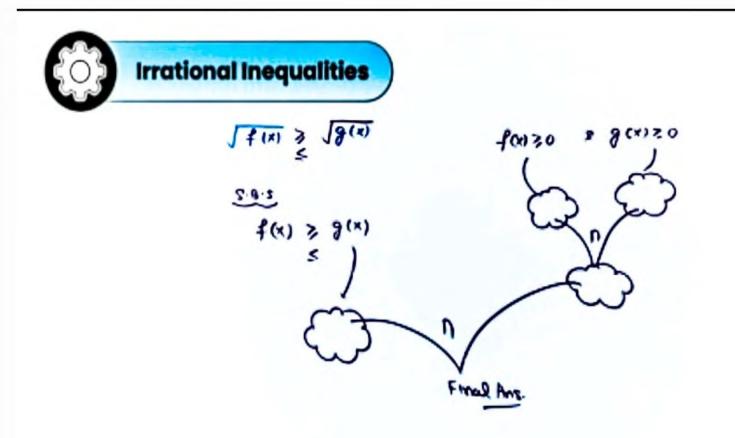


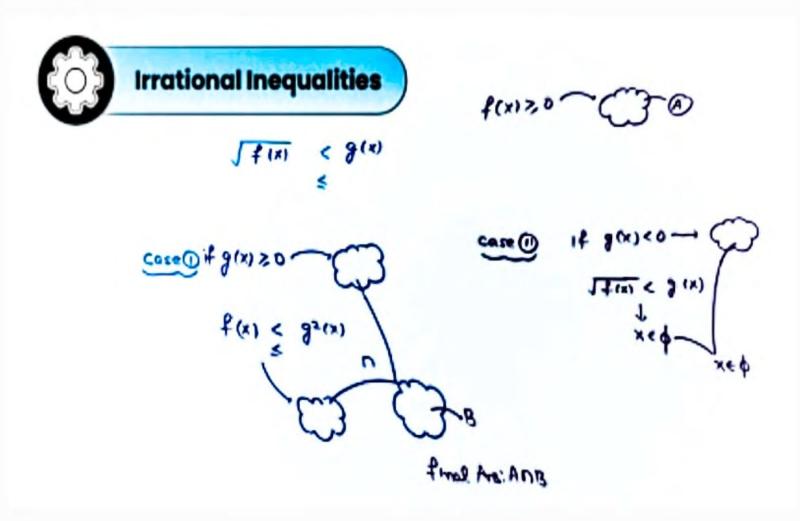
Exponential Inequalities

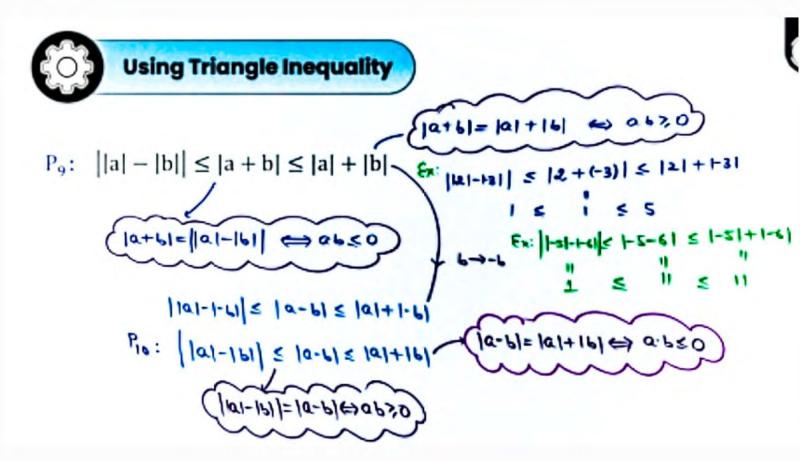


* Incleasing function Kisi bhi inequality mai lagae
HI BEISHI Koi Forak mahi Padtaa
* Decrease Function kisi bhi inequality mai lagae
AT BETSHI sign of inequality is reversed
Inc. Eq:
$$a^{x}(art)$$
, $log_{a}(x)(aro)$
Dec. Eq: $a^{x}(art)$, $log_{a}(x)(aro)$
Dec. Eq: $a^{x}(art)$, $log_{a}(x)(aro)$
 $ki denotes distance blu 0 & x on numberline
eq: $1-3l=3 = 3$
 -3
 $+ [-x]=|x|$, $|x|^{2}=x^{2}$, $|xy|=|x|\cdot|y|$, $|x|=\frac{|x|}{|y|}$, $y=0$, $\sqrt{x^{2}z}[x]$
 $+ 2n[x^{2n}=|x|, x^{2n+1}]x^{2n+1} = x$ $+ |x| px$ $\rightarrow |x|rx \Rightarrow xro$
 $+ 4x| sa, aert \Rightarrow xe[-a;a] + kir a, acres
 $+ a \le 1x| \le b$, $a \ge bert$ $\Rightarrow xe(-\infty, -a] \cup [a, \infty)$$$

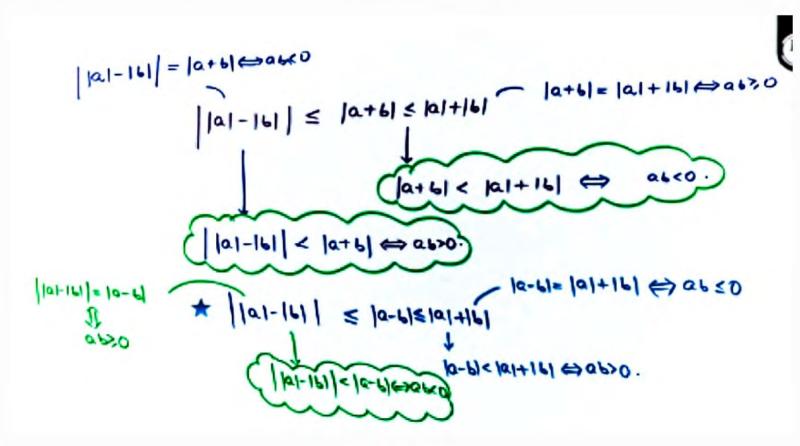


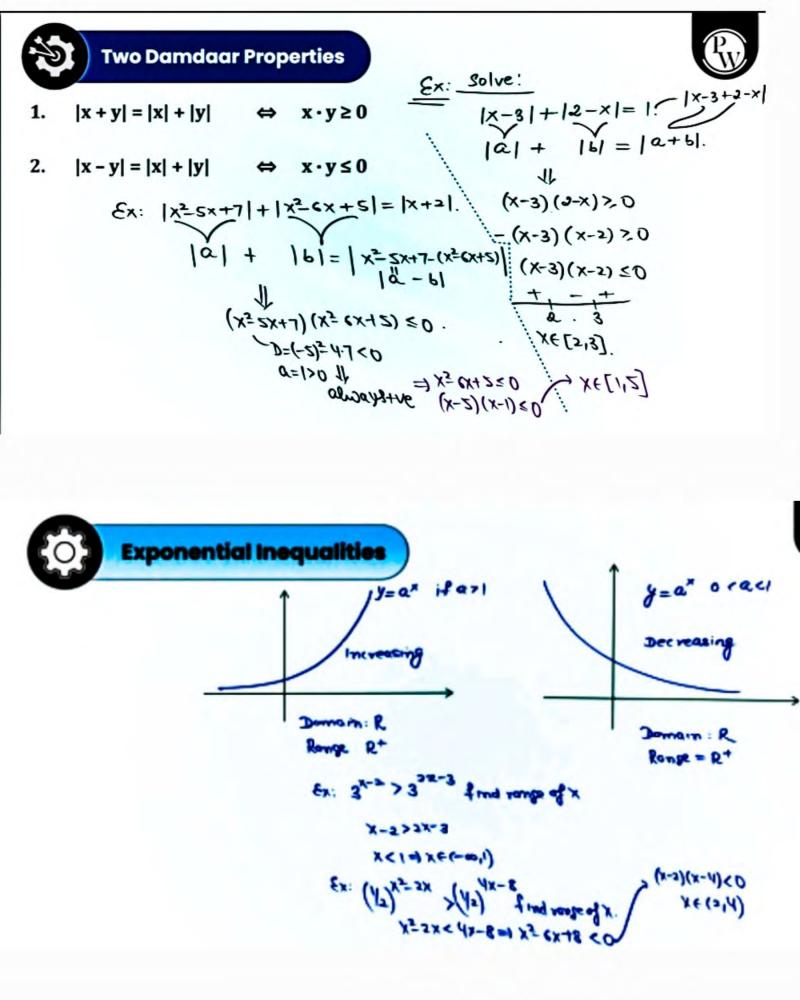






Very important points to Note





Characteristic & Mantissa no: to a given base always has two logarithm of any integral part called characteristic and a fractional part called Mantissa ic e Inter Ex: log 16 = 1,0 / 9 222i Integral port part 0 = azzitmentCharacteristic=4 Ex: find characteristic of log 17 clearly: 24 < 17 < 25 ~ 4 < log 17 < 5 ~ log 17 = 4 characteristic= 4 N KIKAHAANI Ex: log 1 = 0, log 1 = 0 Ex: logo is not defined in real feloil IF OCNCI characteristic $\Rightarrow -1 \le \log_{10} N < 0 \Rightarrow \log_{10} N = -1 + f$ 1≤ N < I -N= 0.689, 0.976 $\downarrow \leq N < \downarrow \implies -2 \leq \log_{10} N < -1 \implies \log_{10} N = -2 + f$ N= 0.078,0.09705 ¥ -2 N= .0018,0.00965 * tan = N<tao = -3 < RogN <-2 = RogN =-3+4 -3 If OCNCI, logN has characteristic= -No: of O's Immediately to right of decimal mN before a +1 steats tight transfinges ***

OQ N KIKAHAANI Ex: log 1 = 0, log 1 = 0 Ex: logo is not defined in reals fe [oi) characteristic 1 N71 $* 1 \le N < 10 \implies 0 \le \log N < 1 \implies \log N = 0 + f$ 0 N= 1.63, 9.85 N= 95.02, 88.55 * 10 < N < 100 = 1 < 000 N<2 =) log N = 1+f N= 110.23,999.25 * 100 ≤ N< 1000 => 2 ≤ log N<3 => log N=2+f L, 19 N>1, logN has characteristic = (NO: of significant digits to left) - 1 gdecimal in N ++++++++ folgettonal Part & [0,1] * logaN = I + (ManHssa) Integer port (charactertstic) negative if N7.1 characteristic of log N * 109 2=0-3010 = (No: of significant digits before) decimal - 1 * 100 3= 6.4771 * log107=0-8451 FORNEI T = 3.14 characteristic of lay N= (No. af zeros immediately after decimal before (Bignificant digits starts +1) 1.57 37/2 2 4.7

***** X, Q, 64I * Q SX 26 No: of possible values of X=6-5 ******** se eak end -a point answer mai shoamil hotaa har , x,a,beI * acxsb No: of possible values of X=6-2 * Q S X S6, X,Q, bEI No: of possible values of x= b-a+1 acxeb, a,b,xEI × No: of Values of X= b-a-1 1 = <u>c</u> a+6 Q-6 - C-C C+0 prnendo Dividendo atb = cta CR. ant - End if 30x+2B=13 find a, B = 4 18 p -2 = B-1 G1 01 k,a,theb that = = = $\frac{p_{-1}}{2} = \frac{3u-6+2p-2}{3+4}$ k, a 2+ k 2 6, + K 3 C arthton -- $\frac{o^{1}}{\sigma^{1}} = \frac{o^{2}}{\rho^{1}} = \frac{c^{2}}{c^{2}} =$ = 13-8 = 5/7 03+5++(+x=10 1 B=1+542=1013

The End