



# PRAYAS

## JEE 2025

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Lecture - 05

Physics

### Modern Physics

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# Topics *to be covered*

1

**Atomic Collision**

2

**Energy Level When <sup>ATDB.uno</sup>Mass of Nucleus is Consider**

3

4

The radiation emitted when an electron jumps from  $n = 3$  to  $n = 2$  orbit in a hydrogen atom falls on a metal to produce photoelectrons. The electrons from the metal surface with maximum kinetic energy are made to move perpendicular to a magnetic field of  $(1/320)$  T in a radius of  $10^{-3}$  m. Find (a) the kinetic energy of the electrons, (b) work function of the metal, and (c) wavelength of radiation.

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$$\frac{1240}{\lambda} = 13.6 \left( \frac{1}{2^2} - \frac{1}{3^2} \right) \quad \therefore r = \frac{mv}{qB} = \frac{\sqrt{2m(K.E)_{\max}}}{qB}$$

$$13.6 \times \left( \frac{1}{2^2} - \frac{1}{3^2} \right) = \phi + (K.E)_{\max}$$

$$(K.E)_{\max} = ( ) \text{ J}$$

Electrons in a hydrogen-like atom ( $Z = 3$ ) make transitions from the fourth excited state to the third excited state and from the third excited state to the second excited state. The resulting radiations are incident on a metal plate and eject photoelectrons. The stopping potential for photoelectrons ejected by shorter wavelength is 3.95 eV.

$n=5$

$n=4$

$n=4$

$n=3$

$4 \rightarrow 3$

$$13.6 \times 3^2 \left( \frac{1}{3^2} - \frac{1}{4^2} \right) = \phi + 3.95$$

Calculate the work function of the metal and stopping potential for the photoelectrons ejected by the longer wavelength.

$$13.6 \times 3^2 \left( \frac{1}{4^2} - \frac{1}{5^2} \right) = \phi + (eV_0)$$



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A hydrogen-like atom (atomic number  $Z$ ) is in a higher excited state of quantum number  $n$ . This excited atom can make a transition to the first excited state by successively emitting two photons of energies 10.20 eV and 17.00 eV, respectively.

$n = 2$

$$27.2 = 13.6 Z^2 \left( \frac{1}{2^2} - \frac{1}{n^2} \right) \qquad 10.2 = 13.6 Z^2 \left( \frac{1}{3^2} - \frac{1}{n^2} \right)$$

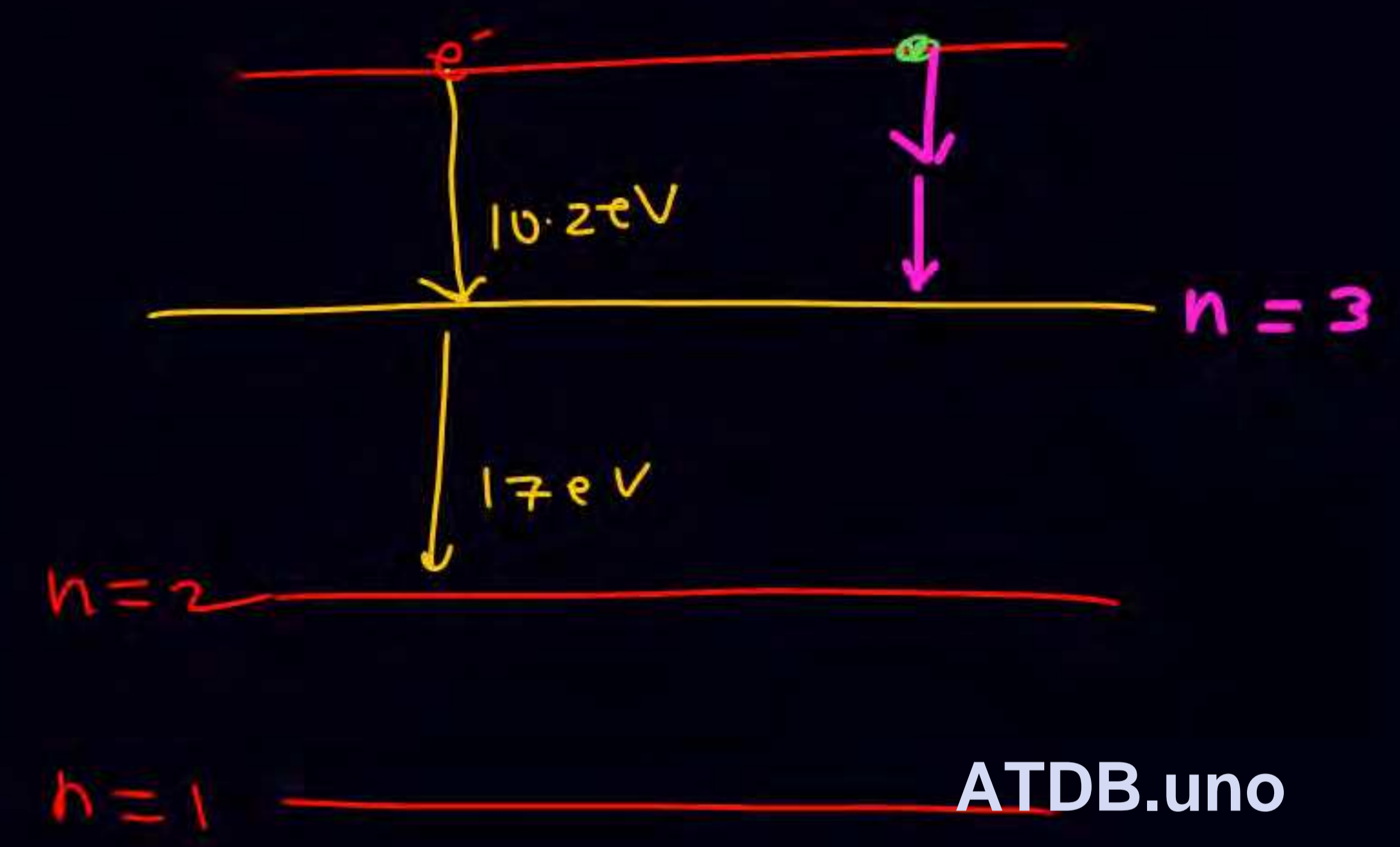
$(n \rightarrow 2)$

Alternatively, the atom from the same excited state can make a transition to the second excited state by successively emitting two photons of energies 4.25 eV and 5.954 eV, respectively. Determine the values of  $n$  and  $Z$  (ionization energy of hydrogen atom = 13.6 eV).

$n \rightarrow 3$

$$\begin{array}{r} 5.954 \\ 4.25 \\ \hline 10.204 \end{array}$$

... to the first excited



A hydrogen-like atom with atomic number  $Z$  is found to be in an excited state corresponding quantum number  $2n$ . It can emit a maximum energy photon of  $204 \text{ eV}$ . If it makes a transition to quantum state  $n$ , a photon of energy  $40.8 \text{ eV}$  is emitted. Find  $n$ ,  $Z$  and the ground state energy (in eV) for this atom. Also, calculate the minimum energy (in eV) that can be emitted by this atom during de-excitation. Ground state energy of hydrogen atom is  $-13.6 \text{ eV}$ .

$$204 = 13.6 Z^2 \left( \frac{1}{1^2} - \frac{1}{(2n)^2} \right)$$

$$40.8 = 13.6 Z^2 \left( \frac{1}{n^2} - \frac{1}{(2n)^2} \right)$$



$$\frac{204}{40.8} = \frac{13.6 z^2 \left( \frac{1}{z^2} - \frac{1}{(2n)^2} \right)}{13.6 z^2 \left( \frac{1}{n^2} - \frac{1}{(2n)^2} \right)}$$

$$5 = \frac{(4n^2 - 1)}{4n^2} \quad \text{ATDB.uno}$$

$\swarrow$   $\searrow$   
 $\frac{3}{4n^2}$

$$\frac{1}{n^2} - \frac{1}{4n^2}$$

$$15 = 4n^2 - 1$$

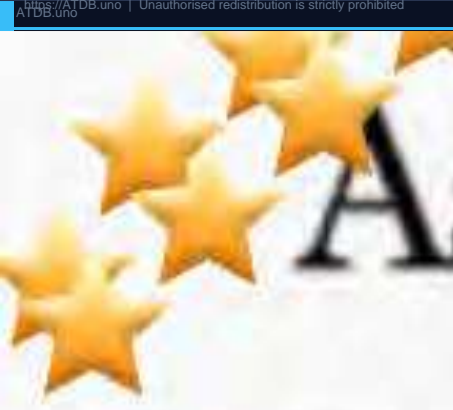
$$16 = 4n^2$$

$$n = 2$$

Brackett series of lines are produced when electrons excited to high energy levels make transitions to the  $n = 4$  level.

- (a) Determine the longest wavelength in this series.  $(\Delta E)_{\min}$   
 $5 \rightarrow 4$
- (b) Determine the wavelength that corresponds to the transition from  $n_f = 6$  to  $n_i = 4$ .  
 $13.6 \times 1^2 \left( \frac{1}{4^2} - \frac{1}{5^2} \right)$

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Assume that the potential energy of a hydrogen atom in its ground state is zero. Then its energy in the first excited state will be:

- A. ~~23.8eV~~
- B. 27.5eV
- C. 30.4eV
- D. 34.8eV

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$z=1$

इसमें जो पद हैं

$n = \infty$  पर  $PE = 0$

$TE = -3.4$   
 $KE = 3.4$   
 $PE = -6.8$

$KE = 3.4$

$PE_{नए} = -6.8 + 27.2 = 20.4$

$n=2$

$TE = 23.8$

$TE = -13.6$   
 $KE = 13.6$   
 $PE = -27.2$

$n=1$

$PE = 0$   
 $KE = 13.6$

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$TE = 13.6$

$+27.2$

10



$z=1$

Let P.E at  $n=2$  is taken as zero  
find T.E at  $n=1$

$n = \infty$  पर P.E = 0  
इसने जो पदा हैं

पुराना  
↓

नया  
↓

T.E = -3.4  
K.E = 3.4  
P.E = -6.8

P.E = 0  
K.E = 3.4

T.E = -13.6  
K.E = 13.6  
P.E = -27.2

$n=1$

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P.E = -27.2 + 6.8  
K.E = 13.6

20

A doubly ionized lithium atom is hydrogen-like with atomic number 3. Find the wavelength of the radiation required to excite the electron in  $\text{Li}^{++}$  from the first to third Bohr orbit. The ionization energy of the hydrogen atom is 13.6 eV.

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**EXAMPLE 3** Find the kinetic energy, potential energy and total energy in first and second orbit of hydrogen atom if potential energy in first orbit is taken to be zero.

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20. An electron in a hydrogen atom undergoes a transition from an orbit with quantum number  $n_i$  to another with quantum number  $n_f$ .  $V_i$  and  $V_f$  are respectively the initial and final potential energies of the electron. If  $\frac{V_i}{V_f} = 6.25$ , then the smallest possible  $n_f$  is.

$$PE \propto \frac{Z^2}{n^2}$$

एक हाइड्रोजन परमाणु का एक इलेक्ट्रॉन  $n_i$  क्वांटम संख्या (quantum number) वाले कक्ष से  $n_f$  क्वांटम संख्या (quantum number) के कक्ष में प्रवेश करता है।  $V_i$  तथा  $V_f$  प्राथमिक एवं अंतिम स्थितिज उर्जाएं हैं। यदि  $\frac{V_i}{V_f} = 6.25$

तब  $n_f$  की न्यूनतम सम्भावी संख्या (smallest possible  $n_f$ ) है। [JEE Advanced-2017]

$$\frac{(PE)_i}{(PE)_f} = \left(\frac{n_f}{n_i}\right)^2 = 6.25$$

$$\frac{n_f}{n_i} = 2.5$$

$$n_f = 2.5 n_i$$

$$n_f = 5$$

$$n_i = 2$$

Ans. 5

27. Consider a hydrogen-like ionized atom with atomic number  $Z$  with a single electron. In the emission spectrum of this atom, the photon emitted in the  $n = 2$  to  $n = 1$  transition has energy 74.8 eV higher than the photon emitted in the  $n = 3$  to  $n = 2$  transition. The ionization energy of the hydrogen atom is 13.6 eV. The value of  $Z$  is.....

$$Z^2 \cdot 13.6 \left( \frac{1}{2^2} - \frac{1}{1^2} \right) - Z^2 \cdot 13.6 \left( \frac{1}{3^2} - \frac{1}{2^2} \right) = 74.8$$

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[JEE Advanced-2018]

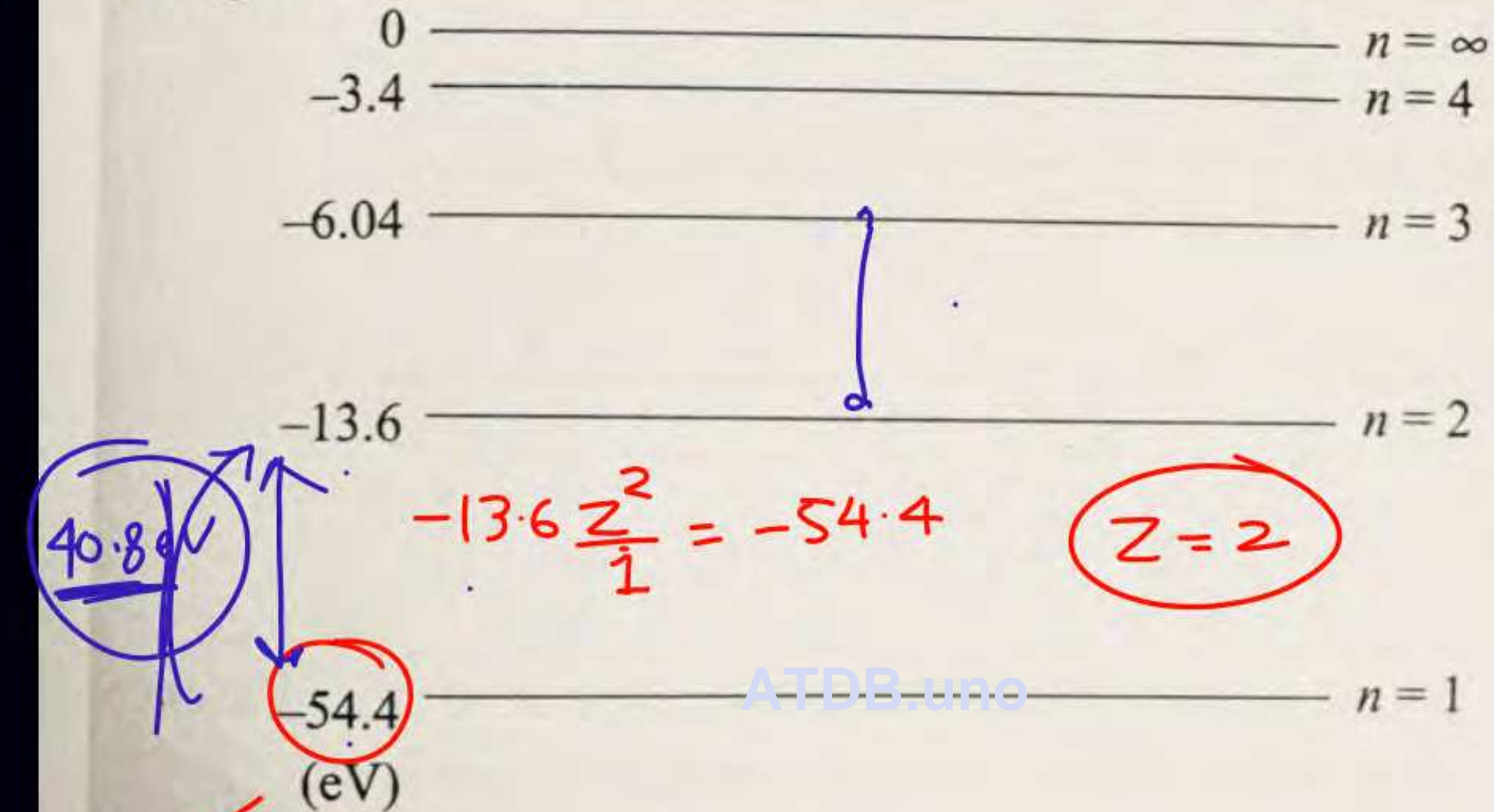
Ans. 3 [3,3]

11. In a photoelectric setup, the radiations from the Balmer series of hydrogen atom are incident on a metal surface of work function  $2\text{eV}$ . The wavelength of incident radiations lies between  $450\text{ nm}$  to  $700\text{ nm}$ . Find the maximum kinetic energy of photoelectron emitted. (Given  $hc/e = 1242\text{ eV}\cdot\text{nm}$ ).
- हाइड्रोजन परमाणु की बॉमर श्रेणी से सम्बन्धित विकिरणों की तरंगदैर्घ्य जो  $450\text{ nm}$  तथा  $700\text{ nm}$  के परास में हैं, एक धातु सतह से फोटो इलेक्ट्रॉन उत्सर्जित करने के लिए प्रयोग किये जाते हैं। धातु का कार्य फलन  $2\text{eV}$  है। उत्सर्जित होने फोटो-इलेक्ट्रॉन की अधिकतम गतिज ऊर्जा ज्ञात करो। (दिया है :  $hc/e = 1242\text{ eV}\cdot\text{nm}$ ) [JEE-2004]

Ans.  $0.55\text{ eV}$

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The energy level diagram for a hydrogen-like atom is shown in figure.



- Find the value of  $Z$ .
- If initially the atom is in the ground state, then
  - determine its first excitation potential, and
  - determine its ionization potential.
- Can it absorb a photon of 42 eV?  $\times$
- Can it absorb a photon of 56 eV?
- Calculate the radius of its first Bohr orbit.
- Calculate the kinetic energy and potential energy of an electron in the first orbit.





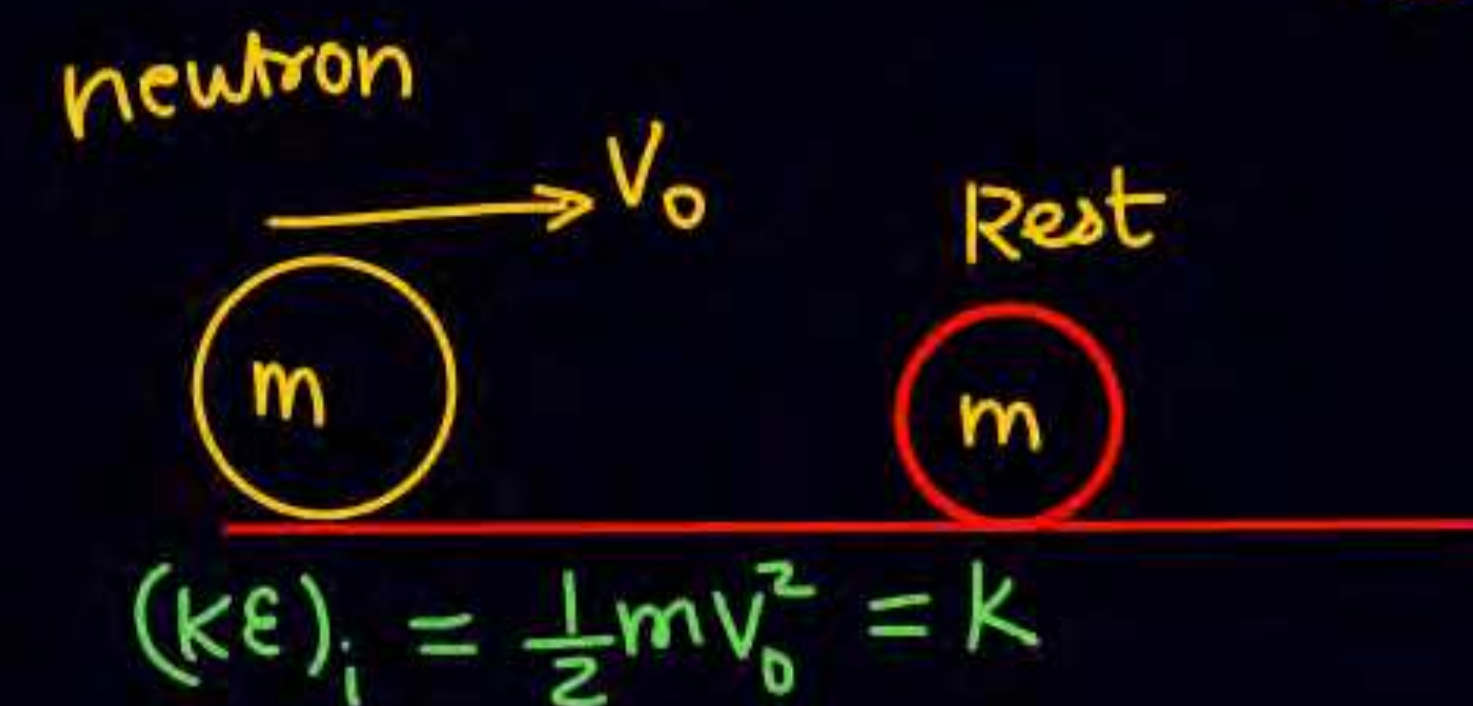
$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

$$e = \frac{v_2 - v_1}{u_1 - u_2}$$

$$|\Delta KE| = \frac{1}{2} \mu u_{rel}^2 (1 - e^2) = \frac{1}{2} \frac{m_1 m_2}{m_1 + m_2} u_{rel}^2 (1 - e^2)$$



## Atomic Collision

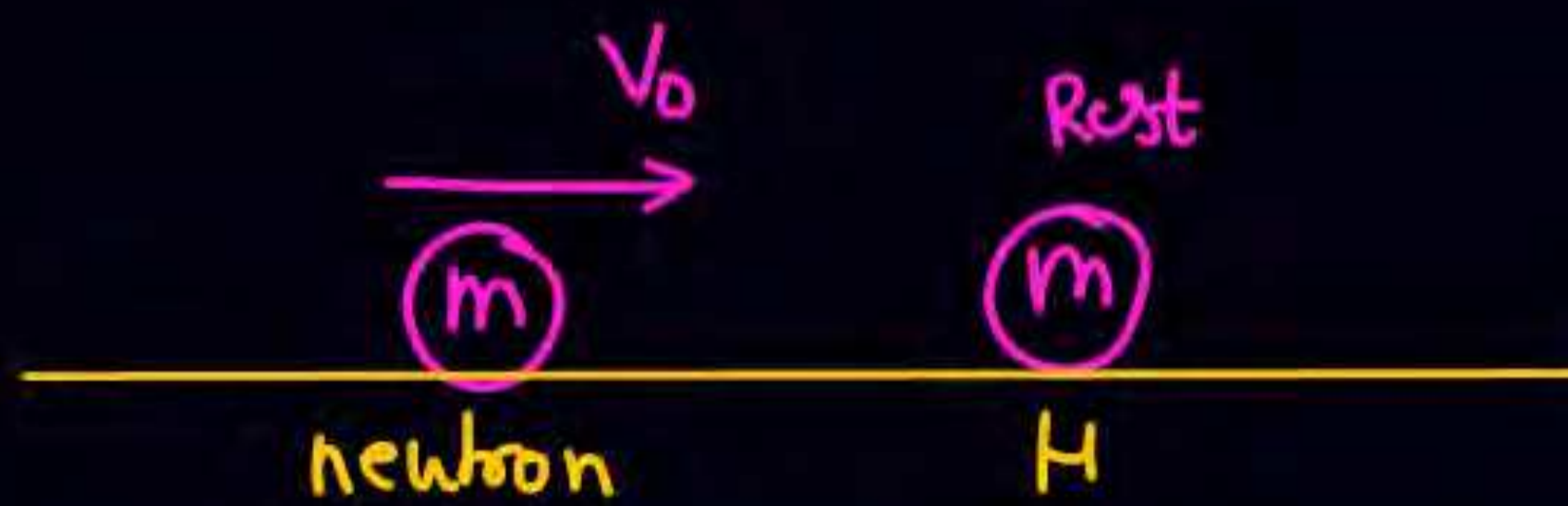


$$(\Delta KE)_{\text{loss}} = \frac{1}{2} \mu u_{\text{rel}}^2 (1 - e^2) \equiv (\text{com में})$$

$$\Delta (KE)_{\text{max}} \equiv \text{loss max possible} \equiv \text{when } e=0 \implies \frac{1}{2} \frac{m m}{m+m} v_0^2 (1 - 0^2) = \frac{1}{2} \left( \frac{1}{2} m v_0^2 \right) = \frac{K}{2}$$

If  $\frac{K}{2} < 10.2 \implies e=1$

$K < 20.4 \implies$  elastic collision



\* max possible loss in KE =  $\frac{K}{2}$  (for  $e=0$ )

\*  $0 \leq (KE)_{loss} \leq (KE)_{max}$

\* If  $\frac{K}{2} < 10.2 \Rightarrow e=1$   
 $K < 20.4 \text{ eV}$

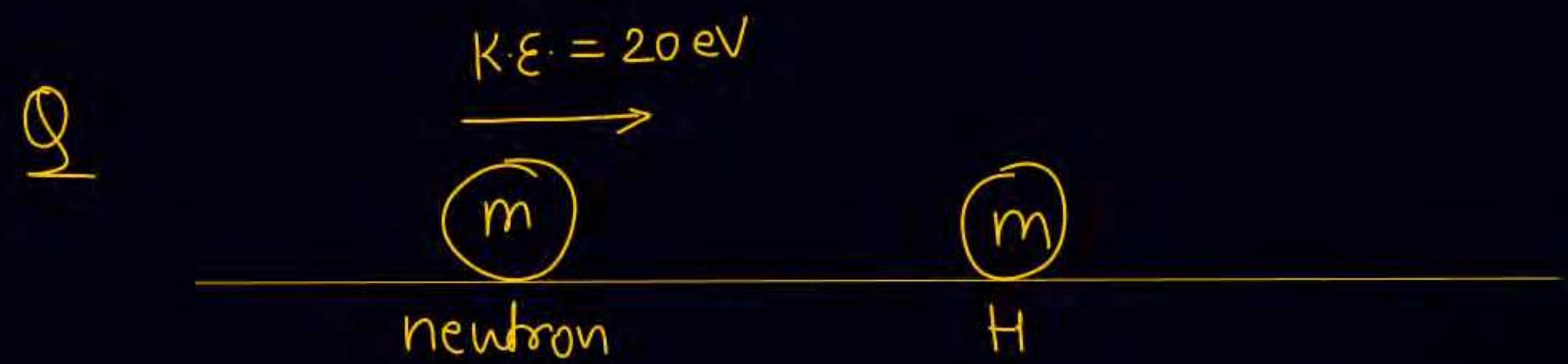
\* SKL का मूल सिद्धांत =



Q find possible value of  $e$  for following cases

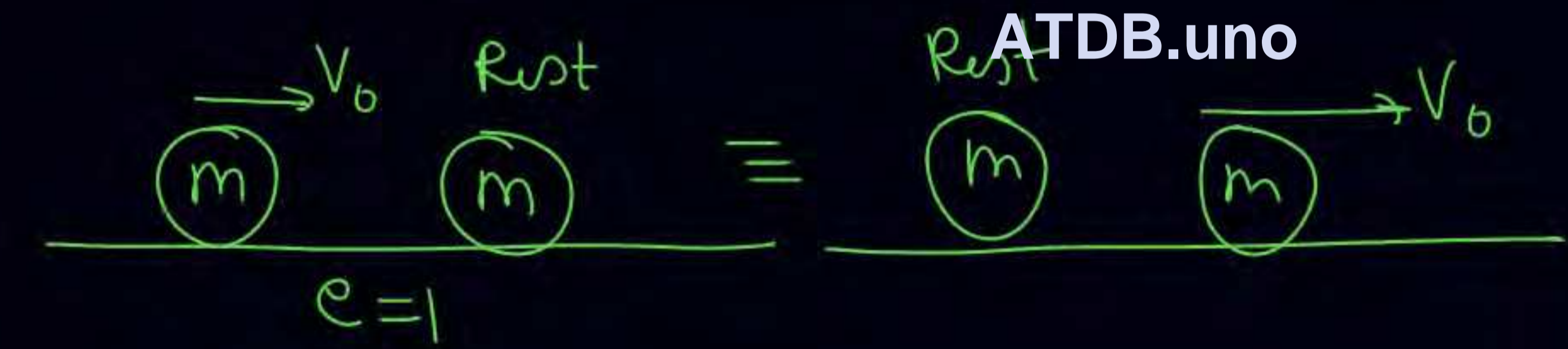
- ①  $K = 10 \text{ eV} \Rightarrow e = 1$
- ②  $K = 20 \text{ eV} \Rightarrow e = 1$
- ③  $K = 20.4 \text{ eV} \Rightarrow e = 1, e = 0$
- ④  $K = 22 \text{ eV} \Rightarrow e = 1, 0 < e < 1, e \neq 0$
- ⑤  $K = 24 \text{ eV} \Rightarrow e = 1, 0 < e < 1, e \neq 0$
- ⑥  $K = 24.18 \text{ eV} \Rightarrow e = 1, 0 < e < 1, e = 0$   
 $\Downarrow$   
 $n=1 \rightarrow n=3$

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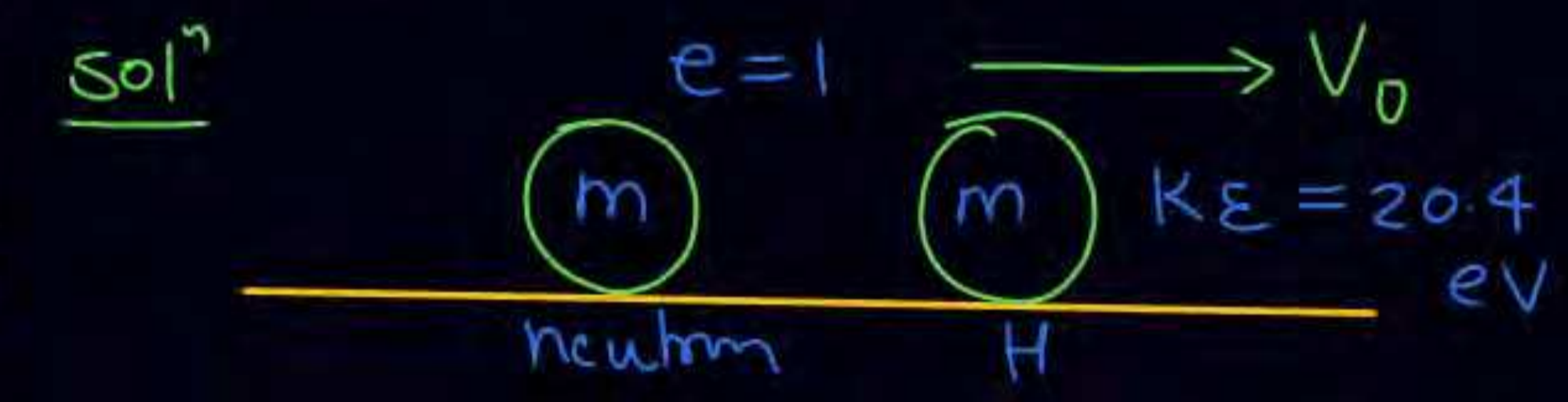
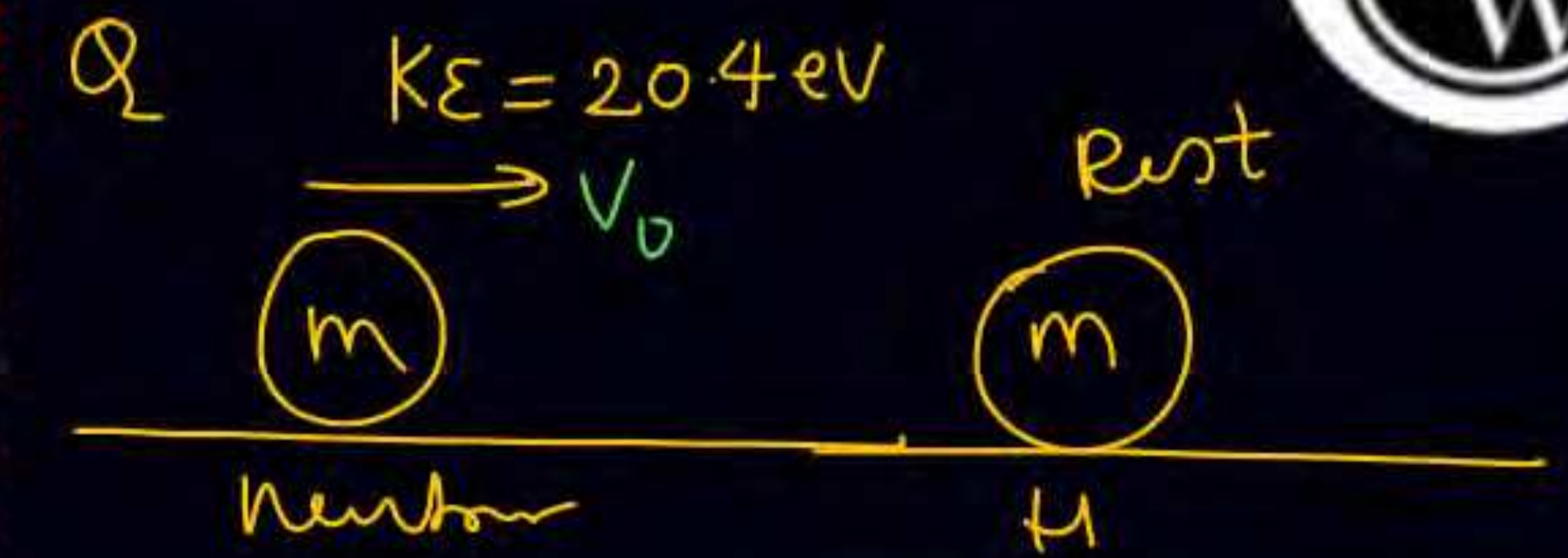


find possible K.E. of H atom after collision

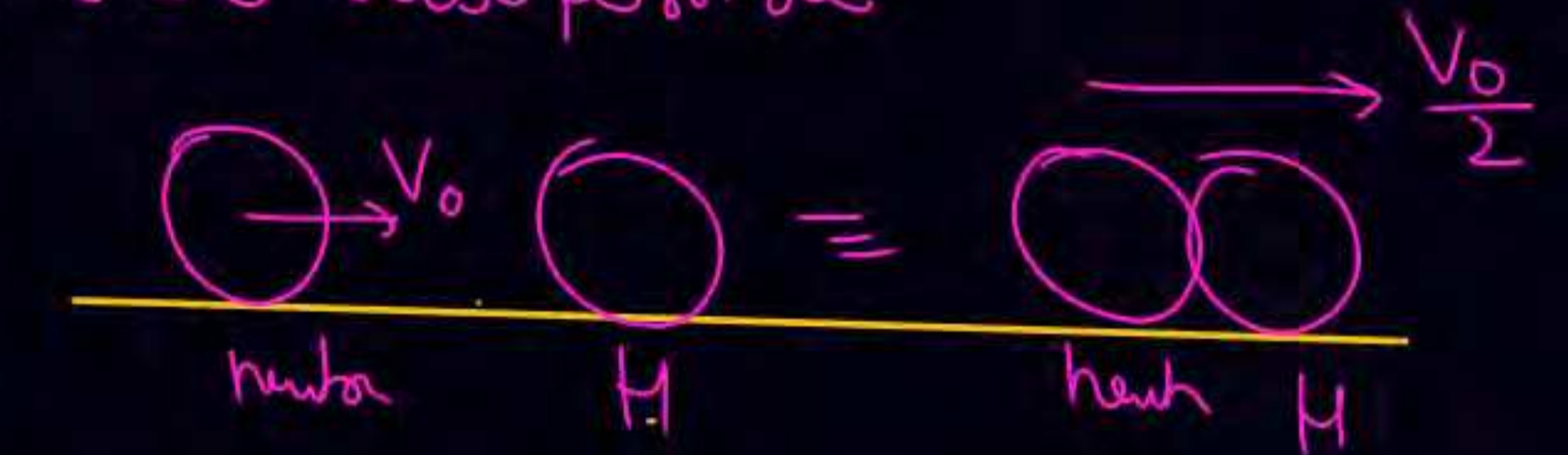
Sol<sup>n</sup>  $K < 20.4 \Rightarrow e = 1$



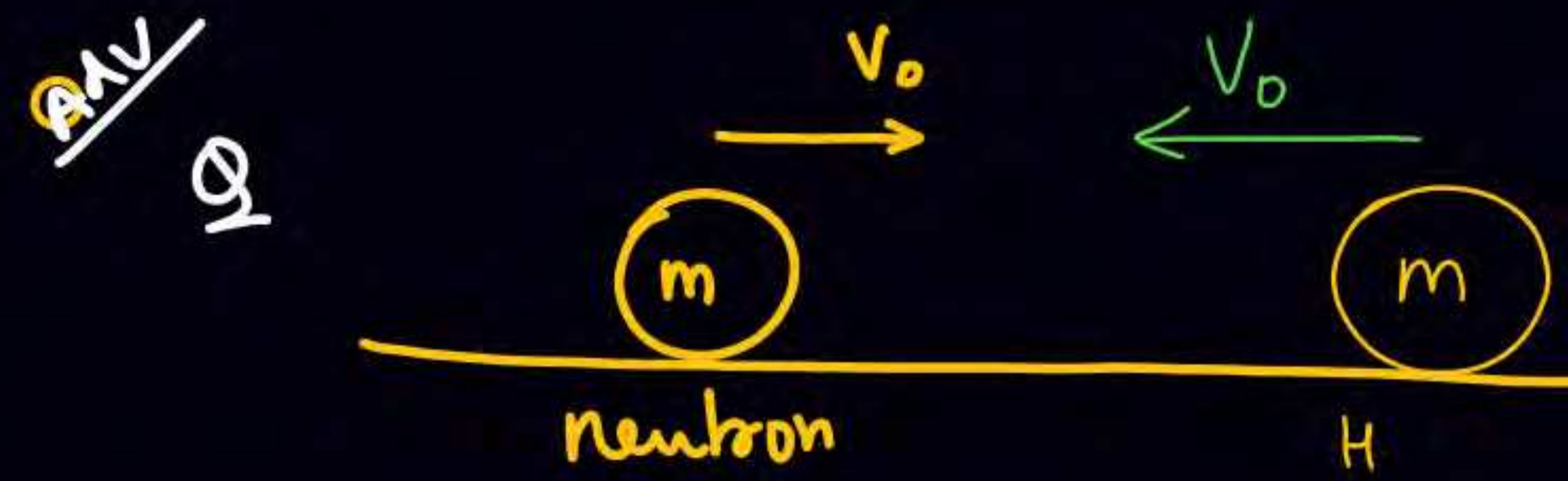
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or  $e = 0$  also possible



(K.E) neutron  $\frac{2}{3} = 5 \cdot 1$   
pass after collision



If KE of both neutron & H is same and 6.4 eV each. find possible KE of neutron or H after collision.

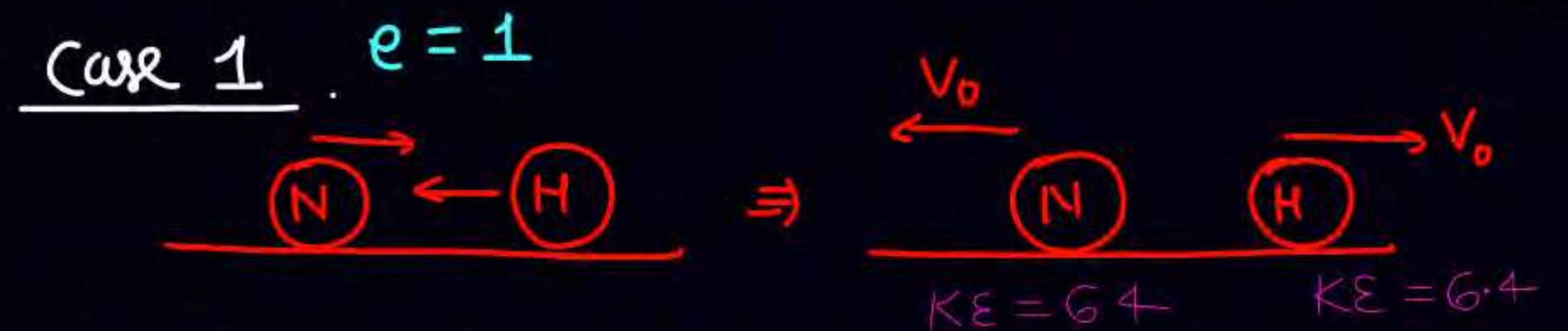
$$(KE)_i = \frac{1}{2}mV_0^2 + \frac{1}{2}mV_0^2 = mV_0^2$$

$$(\Delta KE)_{loss} = \frac{1}{2} \mu u_{rel}^2 (1-e^2)$$

$$\begin{aligned} (max)_{e=0} &= \frac{1}{2} \cdot \frac{m}{2} - (2V_0)^2 (1-0^2) \\ &= mV_0^2 \equiv \text{All initial KE.} \end{aligned}$$



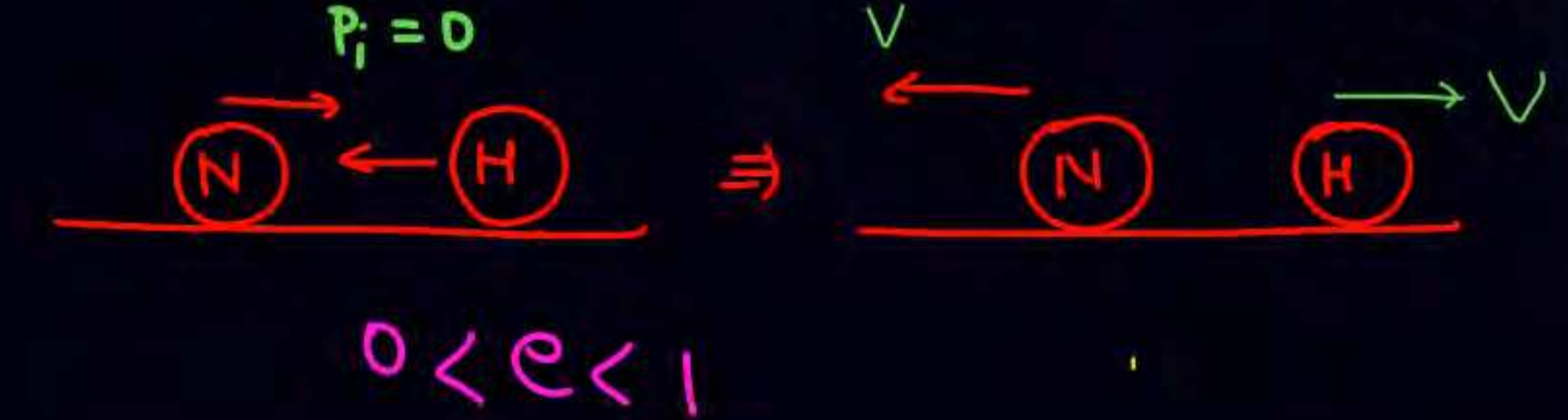
Sol<sup>n</sup> max possible  $(KE)_{loss} = 6.4 + 6.4 = 12.8 \text{ eV}$



Case 2  $10.2 \text{ eV} \Rightarrow e^- \text{ absorbed}$



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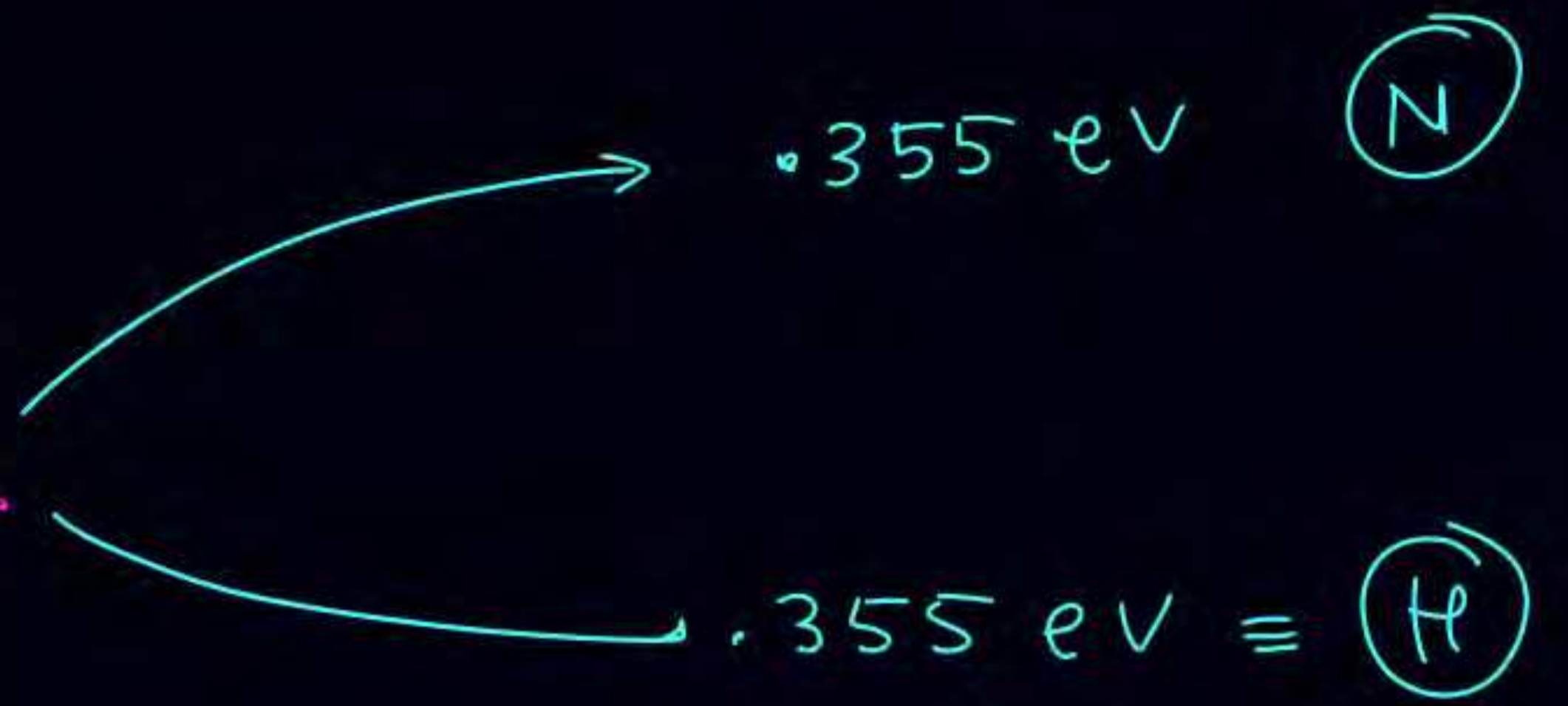




Case 3  $0 < e < 1$

$e^- \Rightarrow 12.09 \text{ eV} \equiv \text{electron absorbed } n=1 \longrightarrow n=3$

(Total K.E)<sub>remain</sub> =  $12.8 - 12.09 = .71$



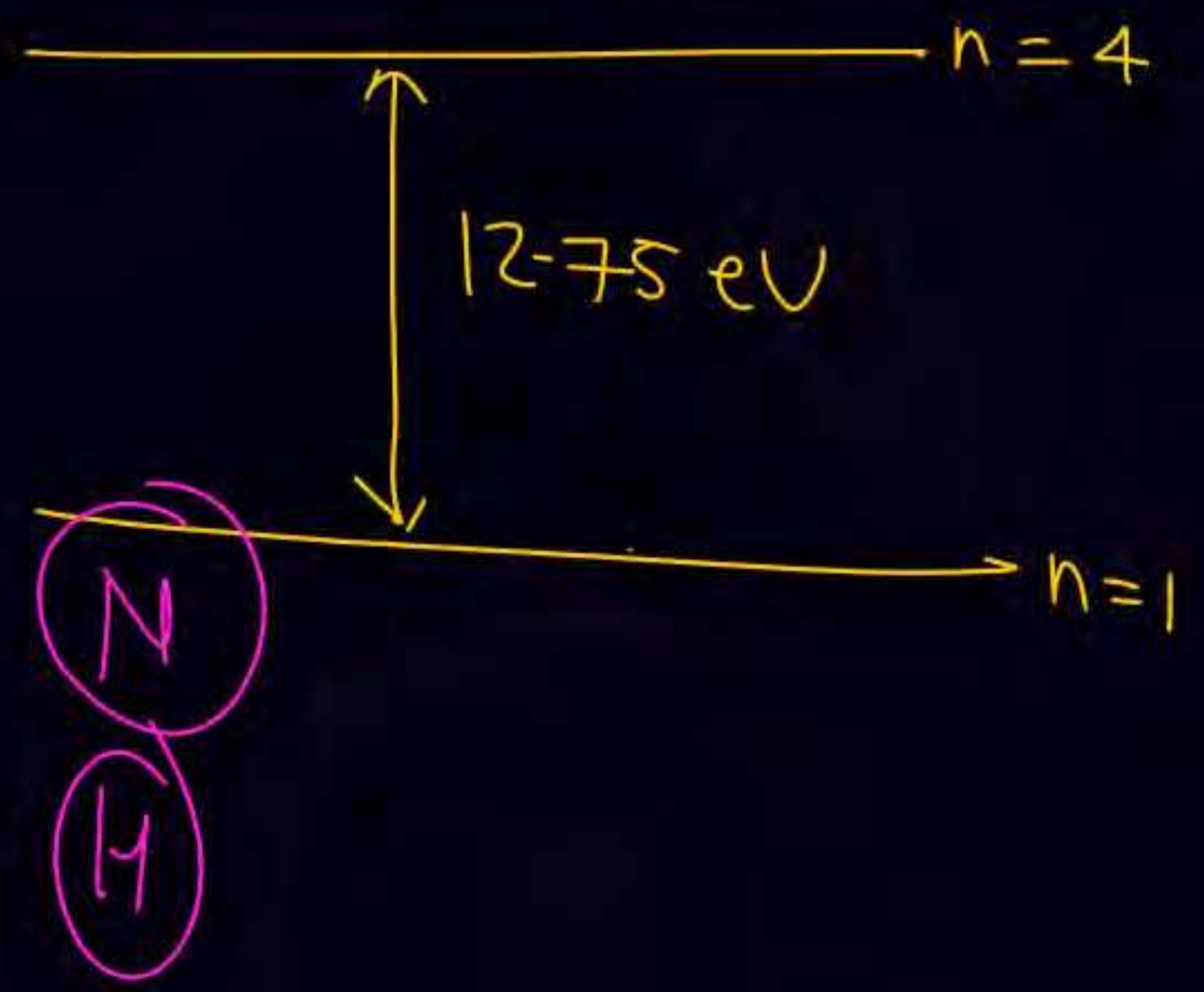
Case 4  $0 < e < 1$

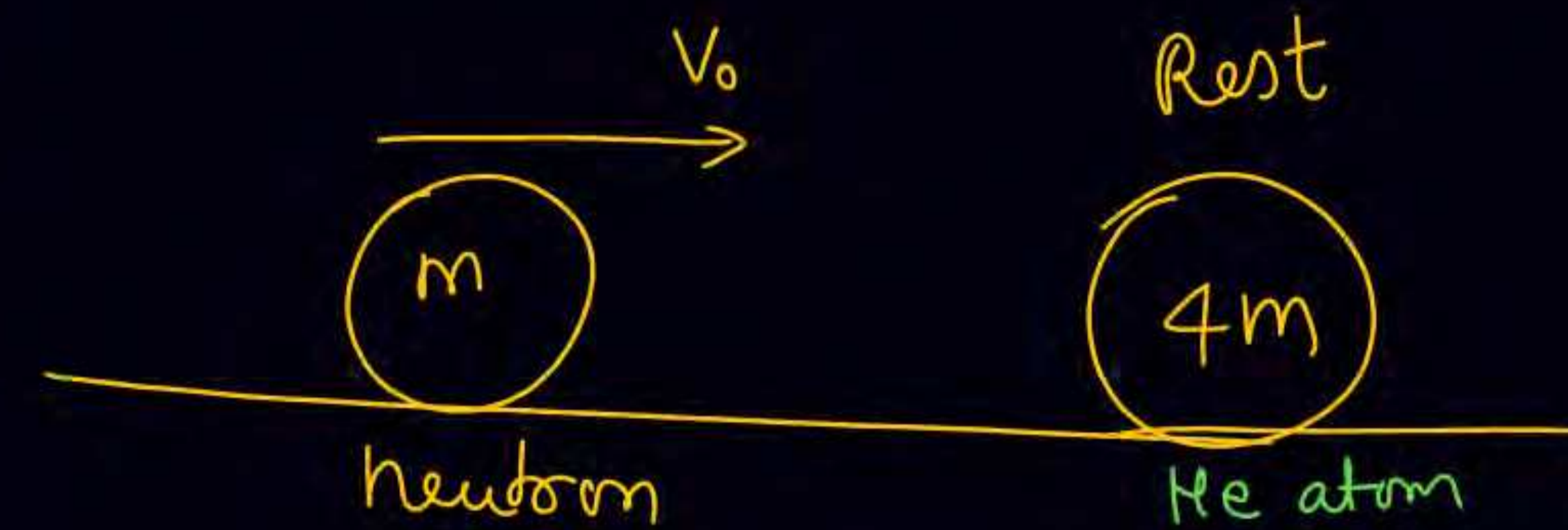
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$e^- \equiv 12.75 \text{ eV} \equiv e^- \text{ absorbed}$

$n=1 \longrightarrow n=4$

(Total KE)<sub>remain</sub> =  $12.8 - 12.75 = .05 \text{ eV}$

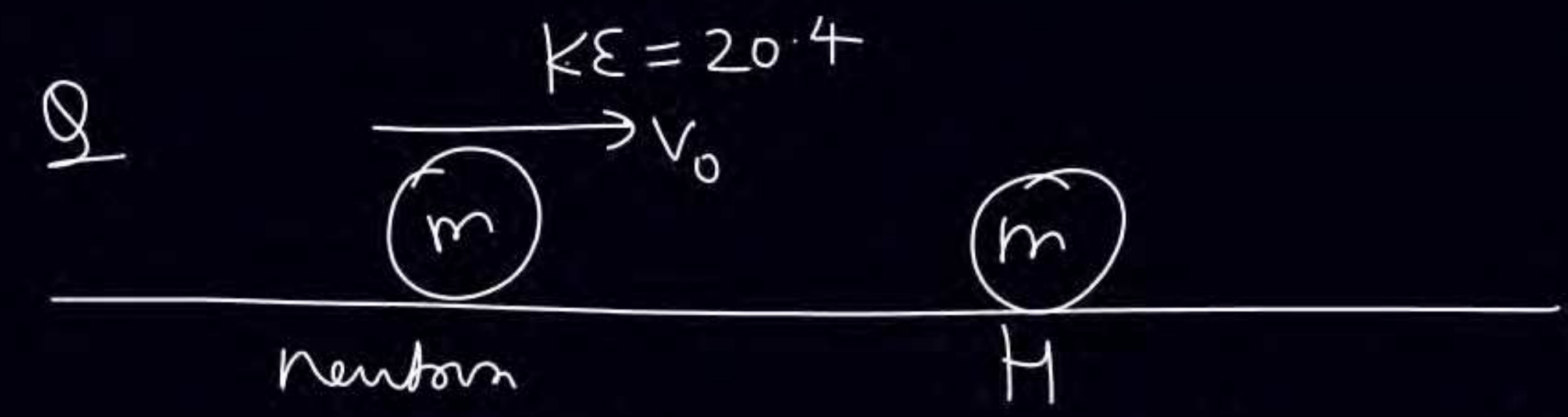




$$\text{If } K = \frac{1}{2} m v_0^2$$

find possible value of  $K$  so that all type of collision may occur!

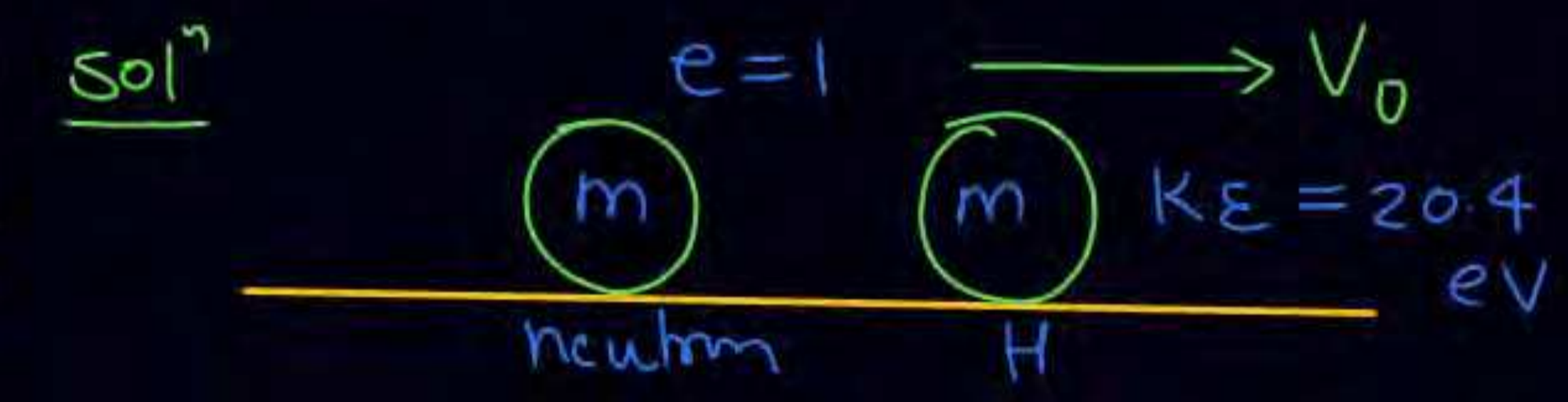
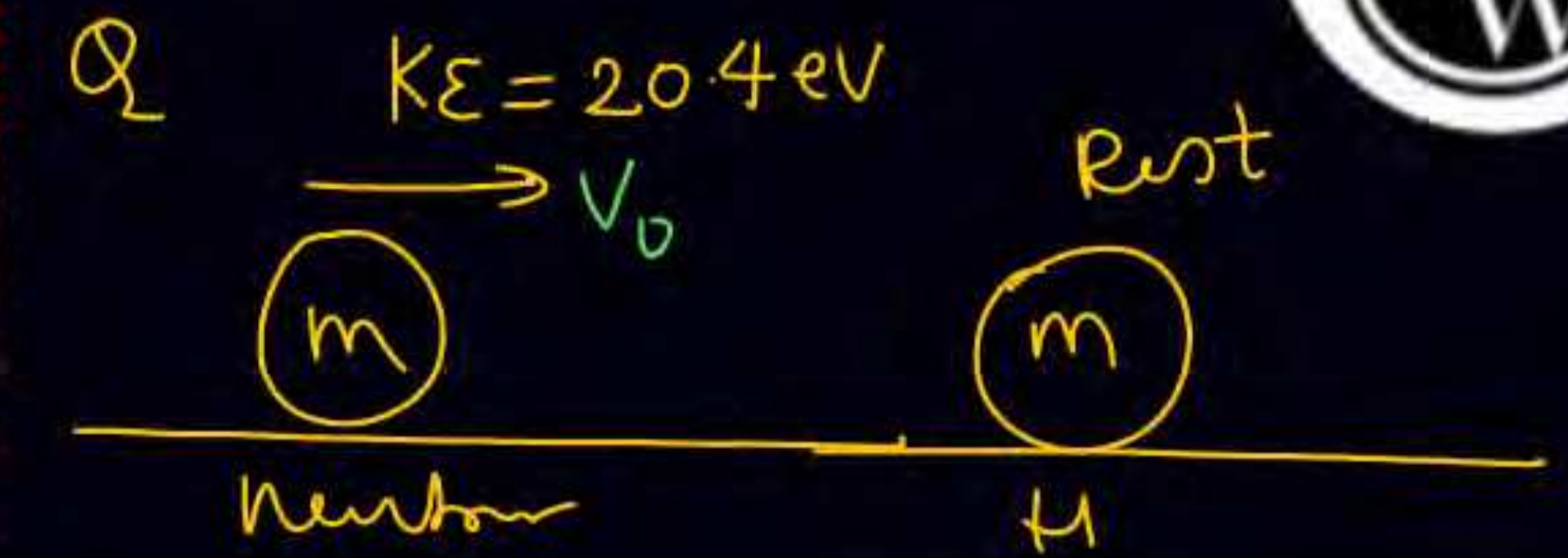




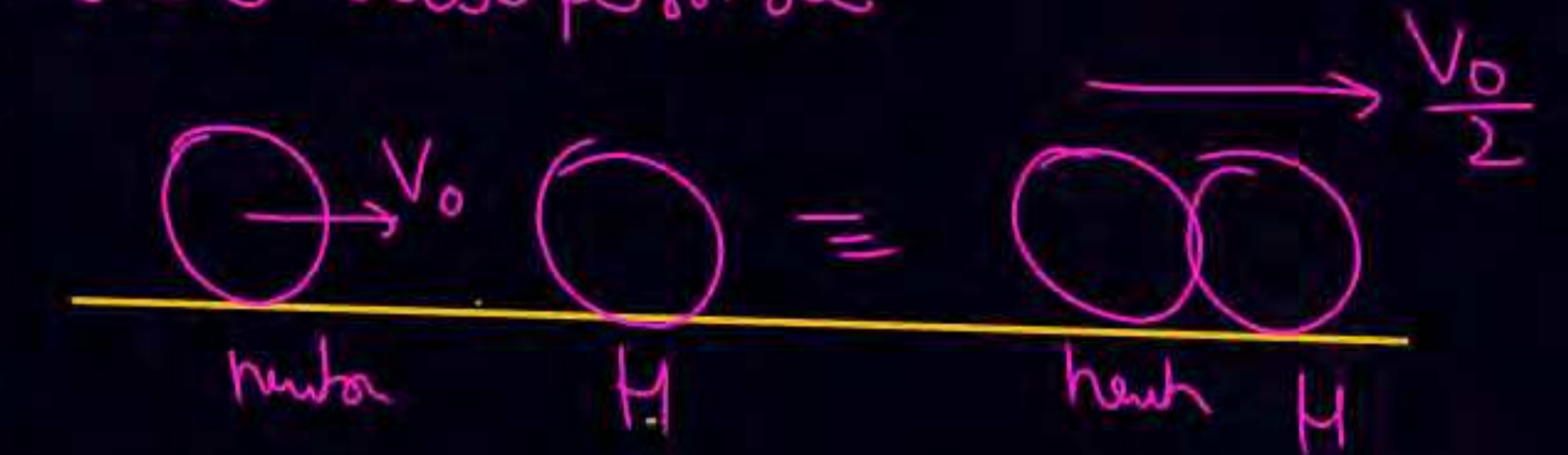
find possible KE of neutron after collision

Sol<sup>n</sup>  $e = 1, KE = 0$   
 $e = 0, KE = 5.1$

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or  $e = 0$  also possible

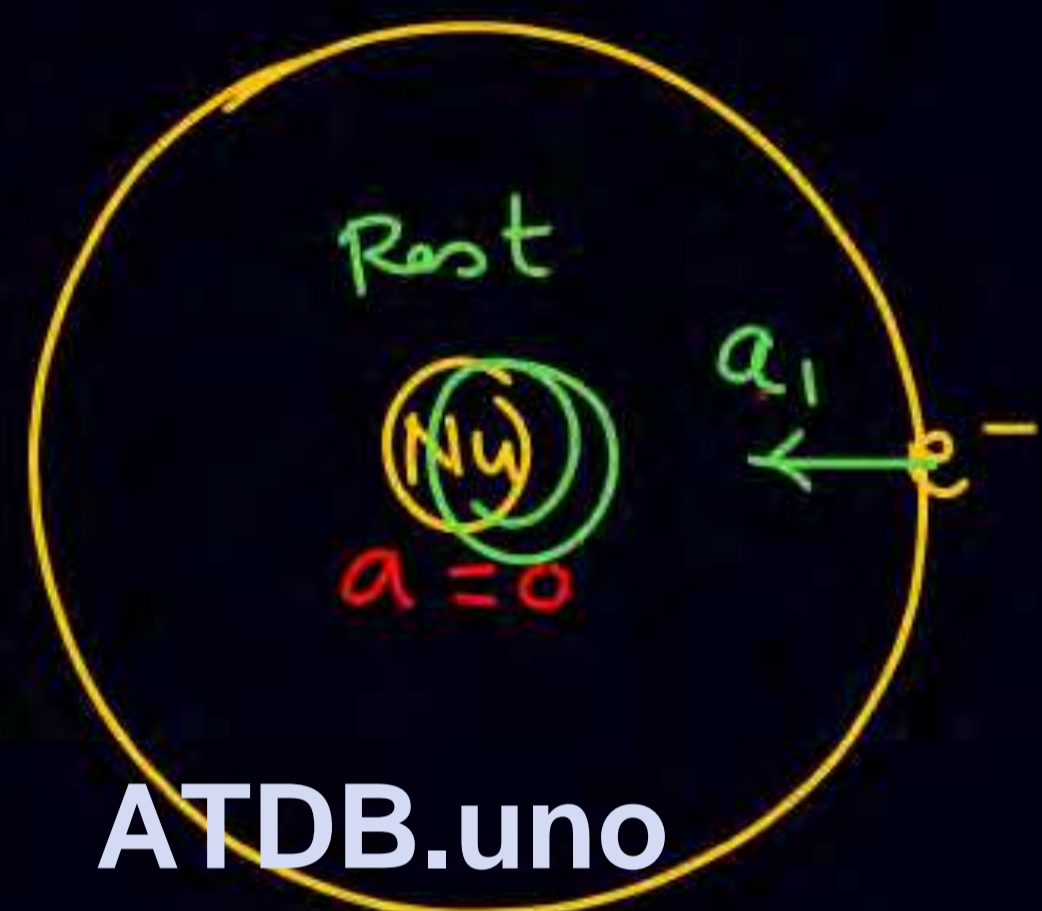


(KE) neutron  $\frac{1}{4} = 5.1$   
 pass after collision



$$F_{net} = 0$$

$$a_{com} = 0$$



$$a_{com} = \frac{m_1 a_1 + m_2 a_2}{m_1 + m_2} = 0$$

$$m_1 \vec{a}_1 + m_2 \vec{a}_2 = 0$$

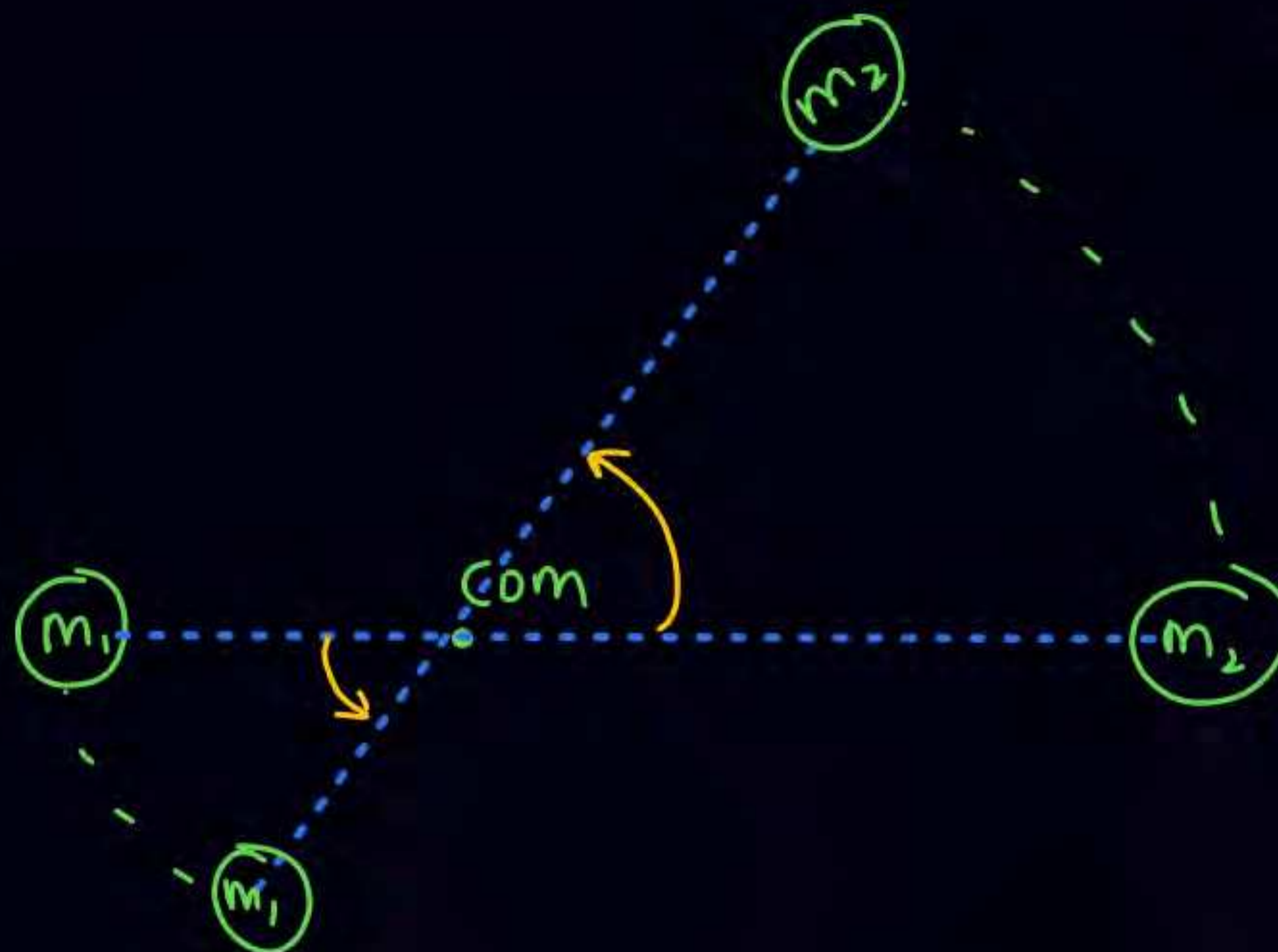
$\parallel$                        $\parallel$   
 $\times$                        $\times$   
 $\Sigma$                        $\Sigma$

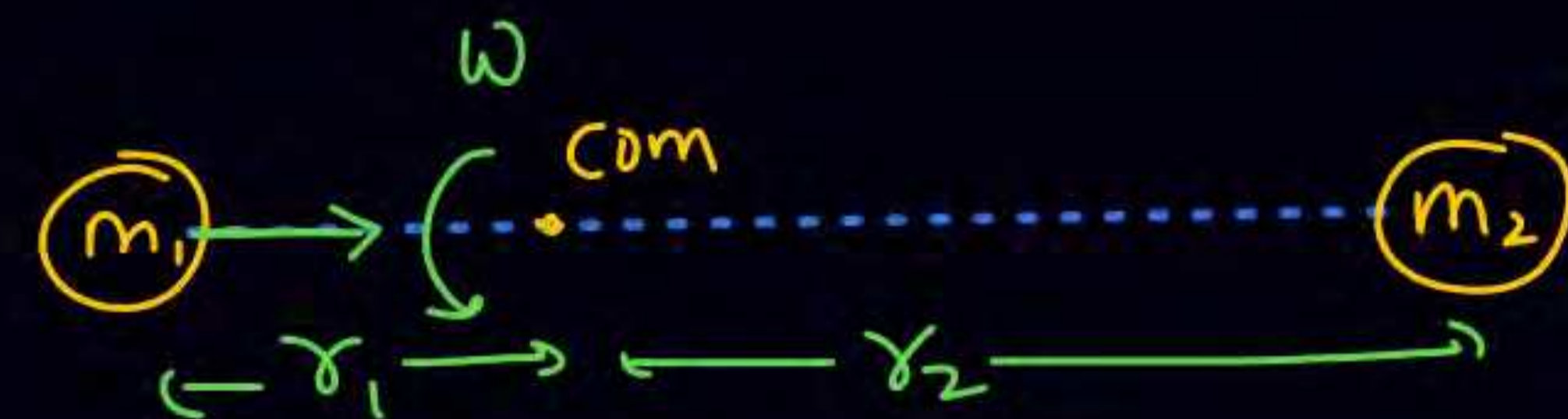


$$F = \frac{kq_1q_2}{r^2} = m_1 r_1 \omega^2$$

$$\frac{kq_1q_2}{r^2} = m_2 r_2 \omega^2$$

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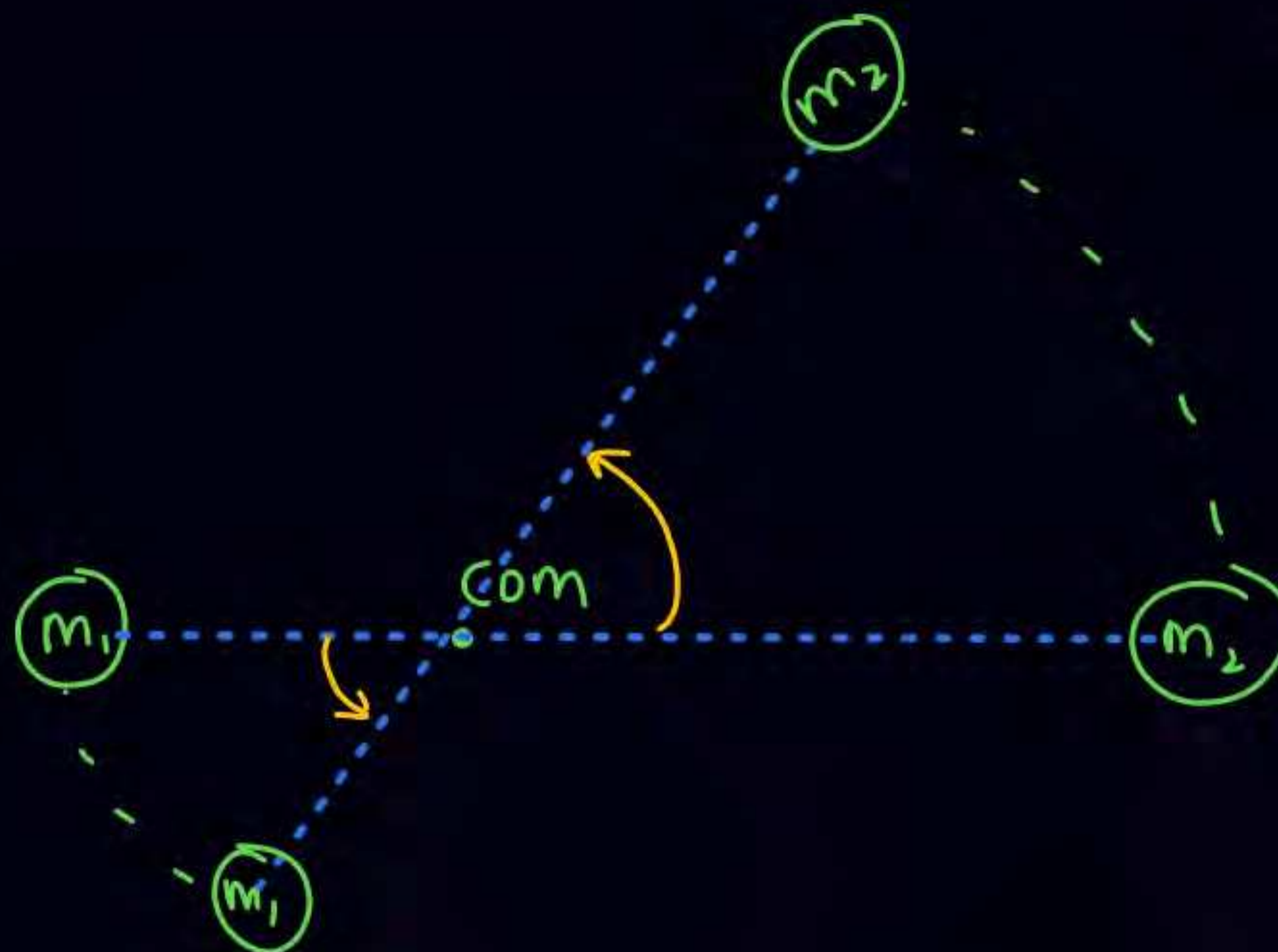




$$\frac{G m_1 m_2}{(r_1 + r_2)^2} = m_1 r_1 \omega^2$$

$$= m_2 r_2 \omega^2$$

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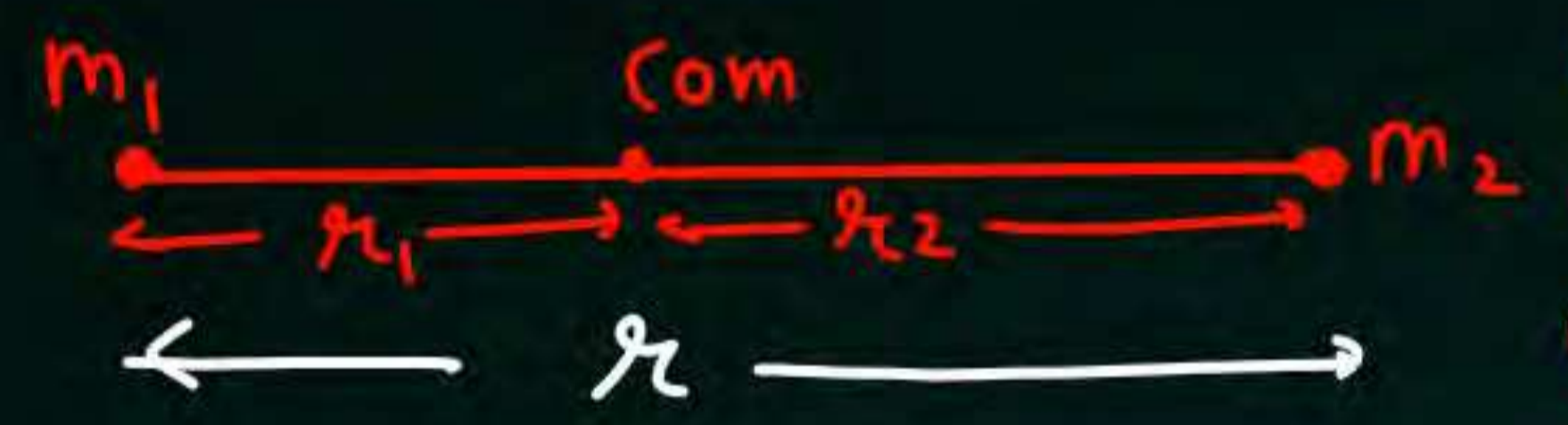
# Effect of nucleus motion

Solve & get

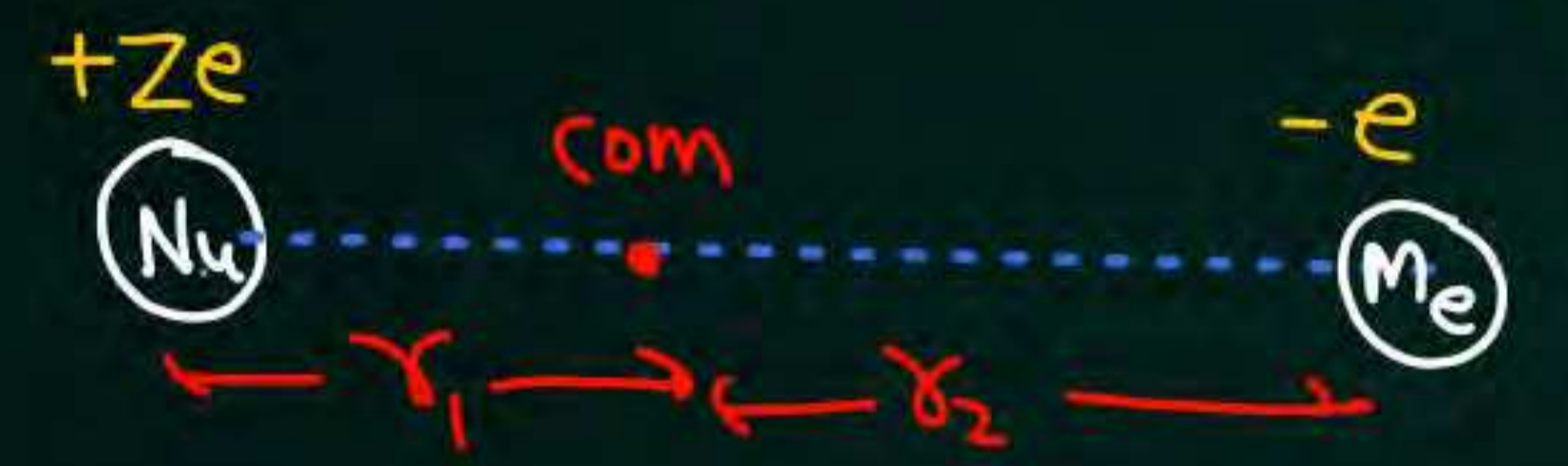
$$\times \frac{Kq_1q_2}{r^2} = m_1 r_1 \omega^2 = m_2 r_2 \omega^2$$

$$\times m_1 v_1 r_1 + m_2 v_2 r_2 = \frac{nh}{2\pi}$$

$$\times m_1 r_1^2 \omega + m_2 r_2^2 \omega = \frac{nh}{2\pi}$$



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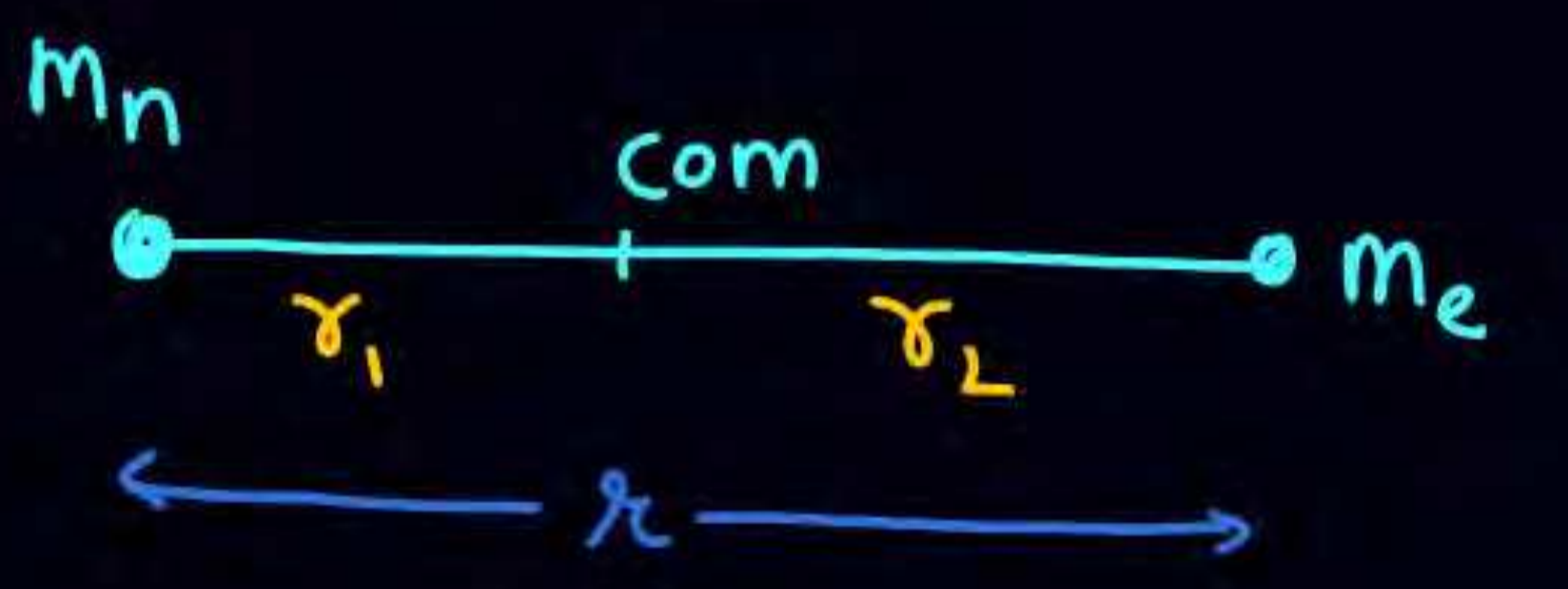
$$r_n = 0.529 \frac{n^2}{Z} \cdot \frac{m_e}{\mu} \rightarrow A^{\circ}$$

$$E = -13.6 \frac{Z^2}{n^2} \cdot \frac{\mu}{m_e} \rightarrow eV$$

$$\mu = \frac{m_1 m_2}{m_1 + m_2}$$



$$r_1 = \frac{m_e r}{m_e + m_n} \quad r_2 = \frac{m_n r}{m_e + m_n} \quad (\text{proof math})$$



$$m_e r_2 \omega^2 = \frac{kze^2}{r^2}$$

$$\frac{m_e m_n r}{m_e + m_n} \omega^2 = \frac{kze^2}{r^2}$$

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$$\mu r \omega^2 = \frac{kze^2}{r^2} \quad \text{--- (1)}$$

$$m_n r_1^2 \omega + m_e r_2^2 \omega = \frac{nh}{2\pi}$$

$$m_n \left( \frac{m_e r}{m_e + m_n} \right)^2 \omega + m_e \left( \frac{m_n r}{m_e + m_n} \right)^2 \omega = \frac{nh}{2\pi}$$

$$\frac{m_n m_e}{m_e + m_n} r^2 \omega = \frac{nh}{2\pi}$$

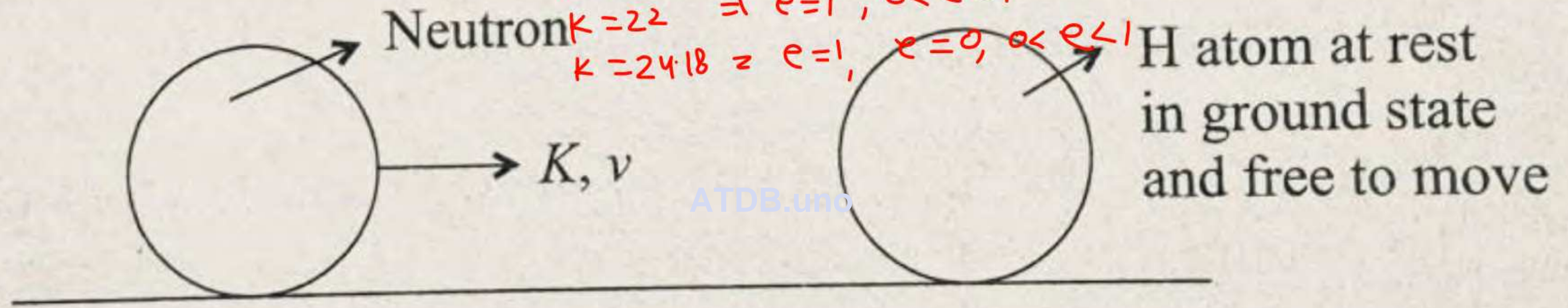
$$\mu r^2 \omega = \frac{nh}{2\pi} \quad \text{--- (2)}$$

Solve (1) & (2)

$$r_n = \left( 529 \frac{n^2}{z} \right) \frac{m_e}{\mu}$$

Q In the figure, what type of collision can be possible, if  $K = 14 \text{ eV}, 20.4 \text{ eV}, 22 \text{ eV}, 24.18 \text{ eV}$  (elastic/inelastic/perfectly inelastic).

$K=14 \Rightarrow e=1$   
 $K=20.4 \Rightarrow e=1, e=0$   
 $K=22 \Rightarrow e=1, 0 < e < 1$   
 $K=24.18 \Rightarrow e=1, e=0, 0 < e < 1$



Head on collision

A He<sup>+</sup> ion is at rest and is in ground state. A neutron with initial kinetic energy  $K$  collides head on with the He<sup>+</sup> ion. Find minimum value of  $K$  so that there can be an inelastic collision between these two particles.



(b)  $K_{\min}$  so that all type of collision are possible



# THANK

# YOU

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