

PRAAAS

JEE 2026

Mathematics

Basic Maths

Lecture - 04

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Topics *to be covered*



- A** Some Important Points
- B** Polynomials and their Factorization



Recap of previous lecture



Fill in the Blanks:

1. If $(x-1)(y-1) = 14$ where $x, y \in \mathbb{I}$ then (x, y) can be _____

$$(x-1)(y-1) = 14$$

2	7	$(3, 8)$
7	2	$(8, 3)$
1	14	$(2, 15)$
14	1	$(15, 2)$
-2	-7	$(-1, -6), (-6, -1)$
-14	-1	$(-13, 0)$
-1	-14	$(0, -13)$

$y-1 = -2$
 $x-1 = -7$

2. If $n = \frac{27}{x} - x$ where $n, x \in \mathbb{N}$ then (n, x) can be $x=1, x=3$
 $n \in \mathbb{N}$ x should be divisor of 27
 $n=26, n=6$ $\rightarrow (26, 1), (6, 3)$

3. 12345x is divisible by 9 then x is 3, 12 $x \in \{0, 1, 2, \dots, 9\}$

4. If 52541x is divisible by 4 then x can be 2, 6

5. $24^2 + 29^2 = \underline{576 + 841 = 1417}$

6. If 6794x is divisible by 6 then x can be 4

$x = \text{even}$ ✓

$26+x$ should be divisible by 3

Recap

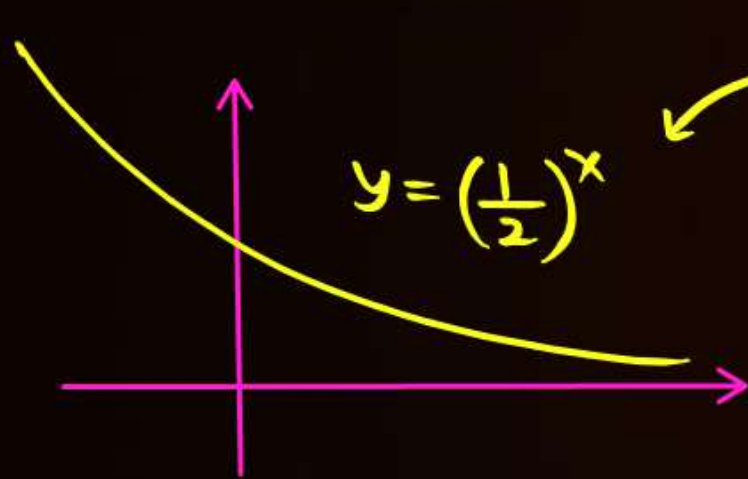
of previous lecture



State True or False

$$(-2)^{-4} = \frac{1}{(-2)^4} = \frac{1}{16} > 0 \quad (0)^4 = 0 \quad \text{neither +ve nor -ve}$$

1. Even power of every real number is always positive. (F) (Any real No:) ^{Even} ≥ 0
2. Odd power of a real number can be positive or negative ^{or zero} depending on number. (T)
3. $x^{2n} \geq 0 \quad \forall x \in \mathbb{R}, n \in \mathbb{N}$ (T)
4. x^{2n+1} is positive if x is positive, $n \in \mathbb{N}$ (T)
5. x^{2n+1} is negative if x is negative, $n \in \mathbb{N}$ (T)
6. If x is a positive real then $x^{\text{any power}}$ is always positive. (T)



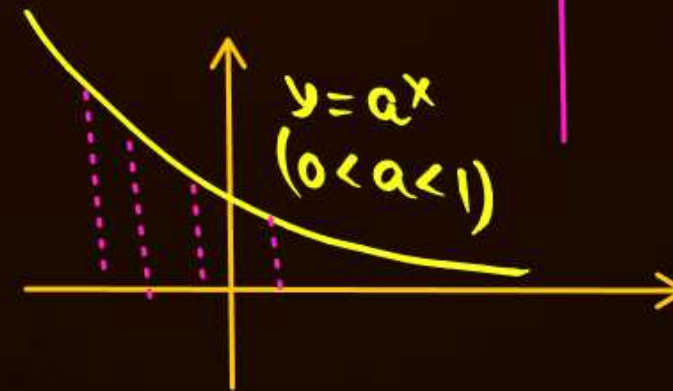
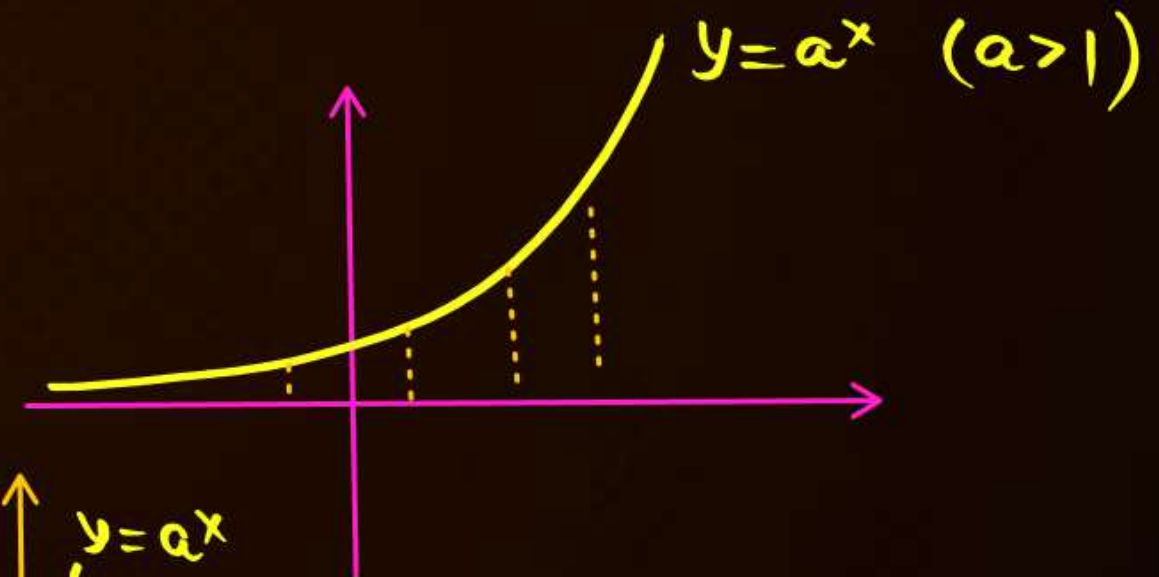
$$\text{Ex: } \left(\frac{1}{2}\right)^x > 0$$

$$\text{Ex: } 2^{-3} = \frac{1}{2^3} = \frac{1}{8} > 0$$

$$\text{Ex: } 7^{-2} > 0$$

$$\text{Ex: } \left(\frac{1}{3}\right)^{-3} = 27 > 0$$

$$\text{Ex: } 3^0 = 1 > 0$$



Recap of previous lecture



7. $x_1^2 + x_2^2 + x_3^2 + \dots + x_n^2 = 0$ where $x_i \in \mathbb{R}$, $i = 1, 2, 3, \dots, n$ then $x_1 = x_2 = x_3 = \dots = x_n = 0$ (T)

8. 6545 is divisible by 7. (T) $654 - 2 \times 5 = 644$
 $64 - 8 = 56$

9. 32436 is divisible by 4, 6 & 9. (T)

10. $55^2 + 44^2 = \underline{3025 + 1936} = 4961$

11. $1 + 3 + 5 + 7 + \dots$ upto 10 terms = $10^2 = 100$

Sum of first n odd numbers = n^2

Ex: $1 + 3 + 5 + \dots$ up to n terms

$$= \frac{n}{2} (2 \cdot 1 + (n-1)2)$$

$$= \frac{n}{2} (2 + 2n - 2) = n^2$$

Homework Discussion

Let a, b, c are real numbers and satisfy $a = 8 - b$ and $c^2 = ab - 16$, then $\frac{a}{b}$ is equal to

$$c^2 = (8 - b)b - 16.$$

$$c^2 = 8b - b^2 - 16$$

$$c^2 + b^2 - 8b + 16 = 0$$

$$c^2 + b^2 - 2 \cdot 4 \cdot b + 4^2 = 0$$

$$c^2 + (b - 4)^2 = 0$$

$$c = 0, b = 4$$

a, b, c are reals such that $a + b + c = 3$ and $\frac{1}{a+b} + \frac{1}{b+c} + \frac{1}{c+a} = \frac{10}{3}$.

The value $E = \frac{a}{b+c} + \frac{b}{c+a} + \frac{c}{a+b}$ is

A 9

~~**B** 7~~

C 5

D 3

$$\downarrow$$
$$\frac{3}{a+b} + \frac{3}{b+c} + \frac{3}{c+a} = 10$$

$$\frac{(a+b)+c}{a+b} + \frac{a+(b+c)}{b+c} + \frac{a+b+c}{c+a} = 10$$

$$1 + \frac{c}{a+b} + \frac{a}{b+c} + 1 + 1 + \frac{b}{c+a} = 10$$

$$\frac{a}{b+c} + \frac{b}{c+a} + \frac{c}{a+b} = 7$$

$$\frac{x}{a+b} \neq \frac{x}{a} + \frac{x}{b}$$

Gadho/Gadhiyoo aisa
naa karo



Solve the equations : $\begin{cases} 2^x + 3^y = 41 \\ 2^{x+2} + 3^{y+2} = 209 \end{cases}$

Ans. $x = 5$ and $y = 2$

What is the area of an equilateral triangle inscribed in a circle of radius 4 cm?

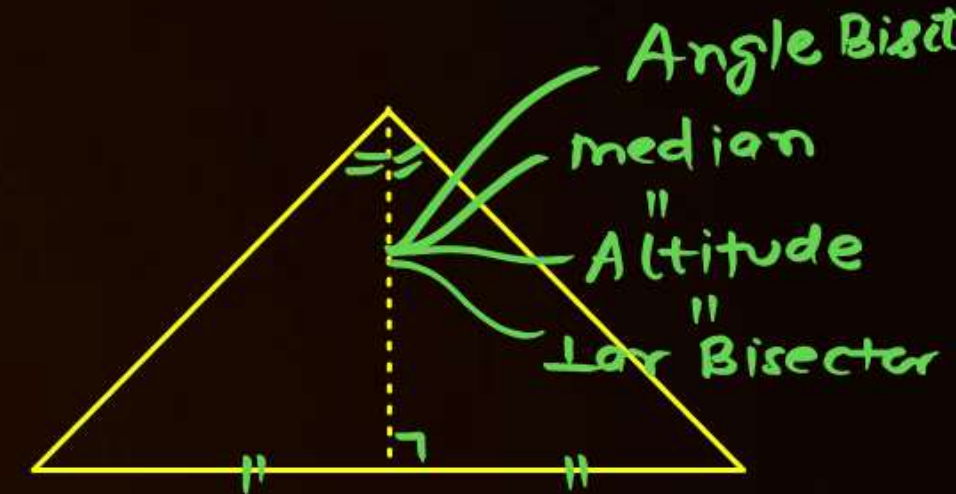
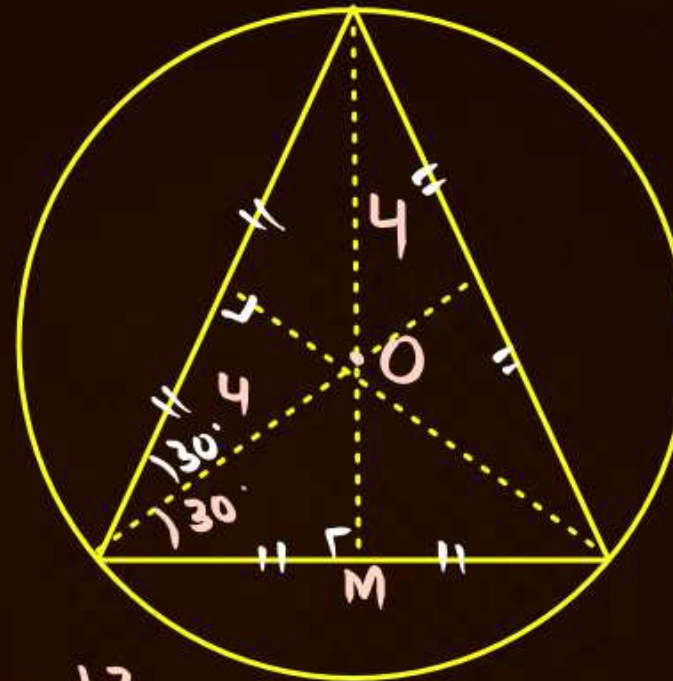
- A** 12 cm^2
- B** $9\sqrt{3} \text{ cm}^2$
- C** $8\sqrt{3} \text{ cm}^2$
- ~~D~~** $12\sqrt{3} \text{ cm}^2$

$$\sin 30^\circ = \frac{OM}{4}$$

$$OM = 4 \sin 30^\circ = 2$$

$$h = 4 + 2 = 6$$

$$\text{Area of Equilateral Triangle} = \frac{h^2}{\sqrt{3}} = \frac{36}{\sqrt{3}} = 12\sqrt{3} \text{ cm}^2$$



Per Bisector of any chord of a circle passes through its centre

**Aao Machaay Dhamaal
Deh Swaal pe Deh Swaal**



Appke Doubts Humaray Solutions



Anshika Shahu • 11 hours ago



sir agr koi homework question nhi ho tb kia google ya kisi aur platform ki hint ke liye help le skte try krne ke liye ya fr chod de ki aap kara doge

2 Same Doubts • 0 Reported

 Mark Popular

Recap

of previous lecture

State True or False

1. Every prime except 2 is odd. (T)
2. Every prime ≥ 5 is of type $6k \pm 1$, $k \in \mathbb{I}^+$. (T)
3. Every number of type $6k \pm 1$, $k \in \mathbb{I}^+$ is prime. (F)
4. Sum of two primes is also a prime. (F)
5. Every composite number has more than two positive factors. (T)
6. Every natural number is either prime or composite. (F)

is within 1000 ft
the coastline.

Doubt 11 hours ago

Prashant

sir $2+3=5$, $2+5=7$ etc.. prime aa to raha

Recap of previous lecture

State True or False

1. Every prime except 2 is odd. (T)
2. Every prime ≥ 5 is of type $6k \pm 1$, $k \in \mathbb{N}$. (T)
3. Every number of type $6k \pm 1$, $k \in \mathbb{N}$ is prime. (F)
4. Sum of two primes is also a prime. (F)
5. Every composite number has more than two positive factors. (T)
6. Every natural number is either prime or composite. (F)

2. 11. 2014, 10:00

 $6K \pm 1$

is written, please
File 1-200-1000000

Doubt

11 hours ago

piyush mishra

sir 2 number me agar k ki jagah per 6 lele toh
 35 ya 37 ayega lekin
 35 prime nahi h

0 Same Doubts

Doubt

21 hours ago

Prakhar

sir 1st me 9 odd hai pr prime nahi hai toh ye false hona chahiye tha?

0 Same Doubts

$2^{2x} - 3^{4y} = 55$
 $(2^x - 3^y)(2^x + 3^y) = 55 = 11 \times 5 = 55 \times 1$
 $(x, y \in \mathbb{I}^+)$

$2^x + 3^y = 11$ $2^x - 3^y = 5$ <hr/> $2 \cdot 2^x = 16$ $2^x = 8$ $x = 3$	OR	$2^x + 3^y = 55$ $2^x - 3^y = 1$ <hr/> $2 \cdot 2^x = 56$ $2^x = 28$ not for any $x \in \mathbb{I}^+$ \therefore No integral soln.
---	----	--

$2^3 - 3^y = 5$
 $8 - 3^y = 5$
 $3^y = 8 - 5$
 $3^y = 3$
 $y = 1$

Doubt

11 hours ago

sir what about -11 & -5

0 Same Doubts



79 hours ago



sir 55 ko 2ke power -3 ke power me express krke compare krke x and y ka value nhi nikal skte ?

0 Same Doubts * 0 Reported

 **Mark Popular**



Appke Doubts Humaray Solutions

Handwritten solution for the equation $2^{2x} - 3^{2y} = 55$. The solution shows that $(x, y) \in \mathbb{Z}^+$ and $(2^x - 3^y)(2^x + 3^y) = 55 = 11 \times 5 = 55 \times 1$. It then considers the cases $2^x - 3^y = 11$ and $2^x - 3^y = 5$, leading to $2^x = 16$ and $3^y = 3$, which gives $x = 4$ and $y = 1$. The final answer is $(4, 1)$.

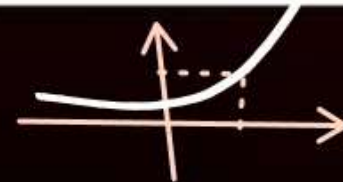
Doubt 11 hours ago

sir agar intejar ke jagah R deta to no of solutions

$$2^{2x} - 3^{2y} = 55$$

If $x, y \in \mathbb{R}$ No: of soln = ∞

$$4^x - 9^y = 55 \Rightarrow 4^x = 55 + 9^y$$



QUESTION

KTK 3

	Column-I	Column-II
(A)	A rectangular box has volume 48, and the sum of the length of the twelve edges of the box is 48. The largest integer that could be the length of an edge of the box, is	(P) 1
(B)	The number of zeroes at the end in the product of first 20 prime numbers, is	(Q) 2
(C)	The number of solutions of $2^{2x} - 3^{2y} = 55$, in which x and y are integers, is	(R) 3
		(S) 4
		(T) 6

Doubt 11 hours ago

sir esma 4ki power x - 9 ki power x = 55 aur fir hit and trial kar lenaga aur sirf ek hi solution milega

QUESTION

★★★★KCLS★★★★

For each positive number x , let $f(x) = \frac{(x+\frac{1}{x})^6 - (x^6 + \frac{1}{x^6}) - 2}{(x+\frac{1}{x})^3 + (x^3 + \frac{1}{x^3})}$. The minimum value of $f(x)$ is

Handwritten solution for the minimum value of $f(x)$. The solution shows that $x + \frac{1}{x} \geq 2$ and $x^3 + \frac{1}{x^3} \geq 2$. It then uses the identity $(x + \frac{1}{x})^3 = x^3 + \frac{1}{x^3} + 3(x + \frac{1}{x})$ to simplify the expression for $f(x)$. The final answer is 6.

Doubt 11 hours ago

sir direct min 2 put karke solve kare to ans 6 hi ara hai pls check

0 Same Doubts



Appke Doubts Humaray Solutions

① $V = lwh = 48$

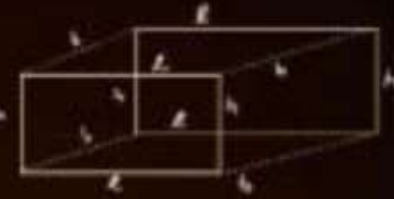
$4(l + b + h) = 48$

$l + b + h = 12$

$l = 12 - b - h$

$l = 12 - b - h$

$l = 12 - b - h$



Doubt

11 hours ago

Sir A nahi samjh aa raha hai aap add aur multiply dono kar rahe hai kyu batayega n

QUESTION

★★★★ KCLS ★★★★★

For each positive number x , let $f(x) = \frac{(x + \frac{1}{x})^6 - (x^6 + \frac{1}{x^6}) - 2}{(x + \frac{1}{x})^3 + (x^3 + \frac{1}{x^3})}$. The minimum value of $f(x)$ is

- (A) 1
- (B) 2
- (C) 3
- (D) 4
- (E) 6

$$\frac{(x + \frac{1}{x})^6 - (x^6 + \frac{1}{x^6}) - 2}{(x + \frac{1}{x})^3 + (x^3 + \frac{1}{x^3})} = 0$$

Doubt

11 hours ago

sir mein yah bhi to kar sakte the ki Main X Plus 1/ x ki minimum value direct likh Li as similarly others mein bhi kar liya and you answer a raha tha vah to sis a raha hai kyunki x positive diya hai toh min 2 max infinity hoti and in denominator same X + 1 by x wali form thi toh fx min krne ke denominator max kr dete fx=0 a jata hope you understand!!

QUESTION

★★★★ KCLS ★★★★★

For each positive number x , let $f(x) = \frac{(x + \frac{1}{x})^6 - (x^6 + \frac{1}{x^6}) - 2}{(x + \frac{1}{x})^3 + (x^3 + \frac{1}{x^3})}$. The minimum value of $f(x)$ is

- (A) 1
- (B) 2
- (C) 3
- (D) 4
- (E) 6

Doubt

11 hours ago

Sir itna bada karne ki kya jarurat hai agar $x^6 + 1/x^6$ woh bhi 2 ke equal ya badi hogi toh harr jagah 2 substitute kardo ans 6 hi aa rahi hai



Appke Doubts Humaray Solutions

QUESTION

★★★★KCLS★★★★

For each positive number x , let $f(x) = \frac{(x+\frac{1}{x})^6 - (x^6 + \frac{1}{x^6}) - 2}{(x+\frac{1}{x})^3 + (x^3 + \frac{1}{x^3})}$. The minimum value of $f(x)$ is

- A 1
- B 2
- C 3
- D 4
- E 6

$$x + \frac{1}{x} = t \quad \text{C8C} \quad x^2 + \frac{1}{x^2} + 3 = \frac{1}{2} \left(x + \frac{1}{x} \right)^2 = \frac{1}{2} t^2$$

$$x^3 + \frac{1}{x^3} + 3t = t^3$$

$$x^6 + \frac{1}{x^6} + 2 = t^6 + 9t^2 - 6t^4$$

$$x^6 + \frac{1}{x^6} = t^6 + 9t^2 - 6t^4$$

$$f(x) = \frac{t^6 + 9t^2 - 6t^4 - 2}{t^3 + t^3 + 3t} = \frac{t^6 + 9t^2 - 6t^4 - 2}{2t^3 + 3t}$$

$$= \frac{6t^4 - 9t^2 - 2}{2t^3 + 3t}$$

$$= \frac{3t^2(2t^2 - 3) - 2}{t(2t^2 + 3)}$$

$$E = 3(t + \frac{1}{t}) \geq 3 \cdot 2 = 6$$

$$E_{\min} = 6$$

Doubt 21 hours ago

Sir numerator minimum aur denominator maximum karne par hoga?

2 Same Doubts



$$\text{min value of } (1a^2 + 3a^2 + 1)(1b^2 + 5b^2 + 1)(1c^2 + 7c^2 + 1)$$

$$a^2 + 3a^2 + 1 \Rightarrow a^2 \left(a^2 + 3 + \frac{1}{a^2} \right) \Rightarrow a^2 \left(a^2 + \frac{1}{a^2} + 3 \right)$$

$$b^2 + 5b^2 + 1 \Rightarrow b^2 \left(b^2 + \frac{1}{b^2} + 5 \right)$$

$$c^2 + 7c^2 + 1 \Rightarrow c^2 \left(c^2 + \frac{1}{c^2} + 7 \right)$$

$$\frac{a^2 b^2 c^2 \left(a^2 + \frac{1}{a^2} + 3 \right) \left(b^2 + \frac{1}{b^2} + 5 \right) \left(c^2 + \frac{1}{c^2} + 7 \right)}{a^2 b^2 c^2}$$

$$\left(a^2 + \frac{1}{a^2} + 3 \right) \left(b^2 + \frac{1}{b^2} + 5 \right) \left(c^2 + \frac{1}{c^2} + 7 \right)$$

$$(2+3)(2+5)(2+7)$$

$$5 \times 7 \times 9 \Rightarrow 315$$

Doubt 21 hours ago

sir a b c ko 1 rakhne pe ans aa ja raha h , is I m wrong anywhere?

0 Same Doubts



QUESTION



Given that $x^2 + y^2 = 8x + 6y + 11$, where x and y are integers. What is the smallest possible value of $|4x - 2y|$.



Diamond Points to Note



P₄: $\sqrt{x^2} = |x|$ Square root of a positive real number is always positive

❖ $\sqrt{\text{Zero}} = \sqrt{0} = 0$

$\sqrt[3]{-8} = -2$, $\sqrt[2]{-4}$ — Not defined in real
 $\sqrt[5]{-32} = -2$

★ \sqrt{x} or $\sqrt[2n]{x}$ is defined in real NO: only if $x \geq 0$

★ \sqrt{x} or $\sqrt[2n]{x} \geq 0 \quad \forall x \geq 0$

★ $\sqrt{x^2} = |x|$, $\sqrt[4]{x^4} = |x|$ —, $\sqrt[2n]{x^{2n}} = |x|$

★ $\sqrt[3]{x}$, $\sqrt[5]{x}$, —, $\sqrt[2n+1]{x}$ is defined $\forall x \in \mathbb{R}$

★ $\sqrt[2n+1]{x} = \begin{cases} +ve & x > 0 \\ -ve & x < 0 \\ 0 & x = 0 \end{cases}$ ★ $\sqrt[2n+1]{x^{2n+1}} = x$

Ex: $\sqrt{(-4)^2} \neq -4$ $\xrightarrow{\text{sahi}}$ $\sqrt{(-4)^2} = |-4| = 4$

b'wz $\sqrt{(-4)^2} = \sqrt{16} = 4$

Ex: $\sqrt[6]{(-3)^6} = |-3| = 3$

Ex: $\sqrt[5]{(-4)^5} = -4$

Ex: $\sqrt[7]{(-6)^7} = -6$

Ex: $\sqrt[3]{2^3} = 2$

$\sqrt{4} = 2$
 ~~$\sqrt{4} = -2$~~

$2n\sqrt{x}$

stands for non -ve
no. whose $(2n)^{\text{th}}$
power is x

$2n+1\sqrt{x}$

stands for a real
no. whose $(2n+1)^{\text{th}}$
power is x



NICHOD!!

➤ $\sqrt[2n]{x} = y \geq 0$ i.e. even root of any non negative real is non negative.

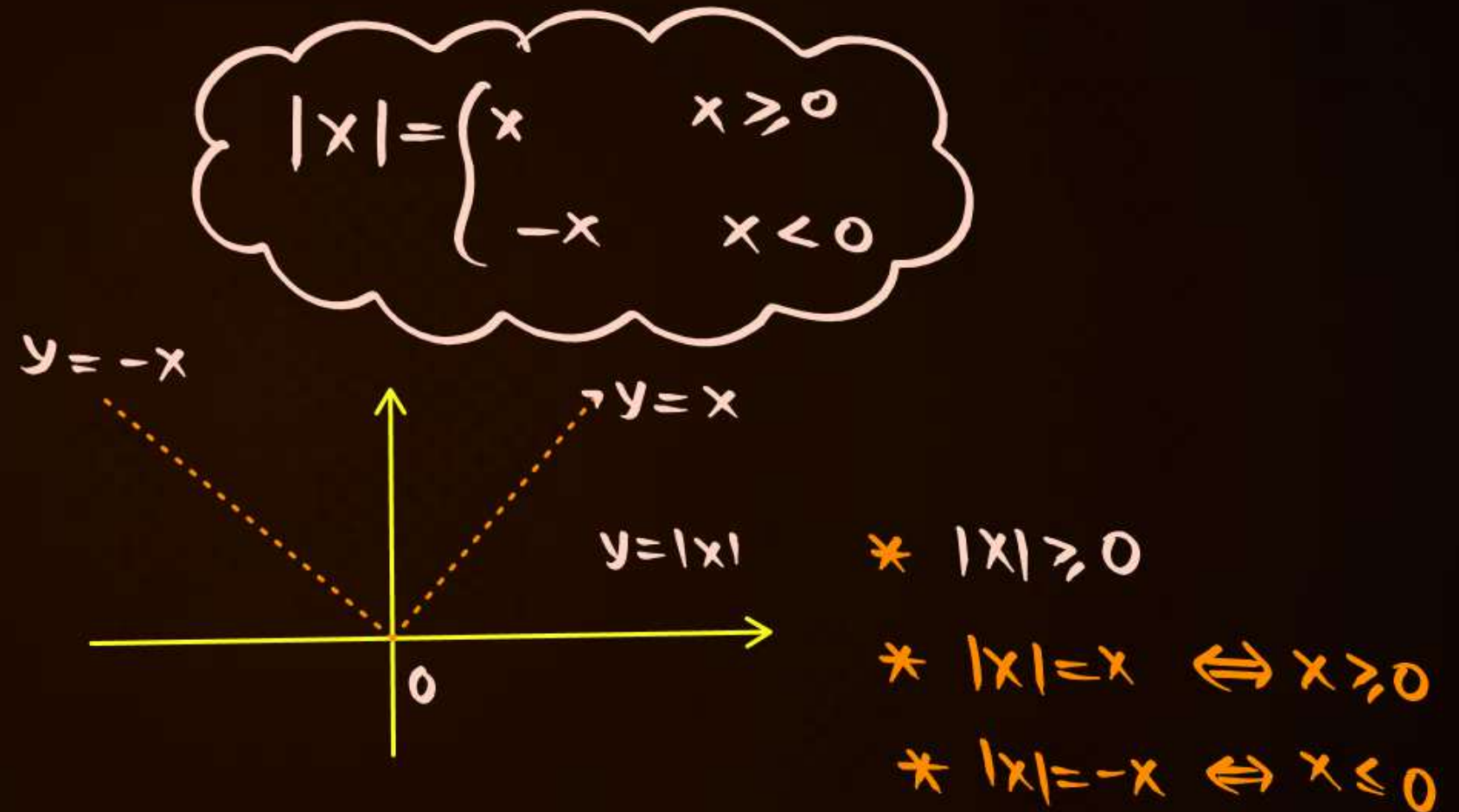
➤ $\sqrt{x^2} = |x|$

➤ $\sqrt[4]{x^4} = |x|, \sqrt[6]{x^6} = |x| \dots\dots\dots$

➤ $\sqrt[2n]{x^{2n}} = |x|, n \in \mathbb{N}$

➤ $\sqrt[3]{x^3} = x, \sqrt[5]{x^5} = x \dots\dots\dots$

➤ $\sqrt[2n+1]{x^{2n+1}} = x, n \in \mathbb{N}$



IQ Test

★ $|x| > x$ if $x \in \underline{(-\infty, 0)}$

★ $|x| < x$ if $x \in \underline{\phi}$

★ $|x| = 2$ if $x = \underline{\pm 2}$

★ $|x| = \sqrt{2}$ if $x = \underline{\pm \sqrt{2}}$

★ $|x| = -1$ if $x = \underline{\text{Not possible.}}$

Ex: $|-2| > -2$
 $|-5| > -5$

$$|-2| = 2 \text{ "School mai"}$$

↓

$$|-2| = -(-2) = 2 \text{ "IIT mai"}$$

↘ -ve

Ex: $-\sqrt{2}$

/

-1.414

$\sqrt{-2}$

\

$(1.414 - j) i$



Yaad Rakhnaa



When quantity inside modulus is non-negative, it comes out as it is, and when the quantity inside modulus is negative, it comes out with minus sign

Teacher

"Find the value of $\sqrt{7 - 4\sqrt{3}} + \sqrt{7 + 4\sqrt{3}}$ "

Kallu: $\sqrt{2^2 + \sqrt{3}^2 - 2 \cdot 2 \cdot \sqrt{3}} + \sqrt{2^2 + \sqrt{3}^2 + 2 \cdot 2 \cdot \sqrt{3}}$
 $\sqrt{(2 - \sqrt{3})^2} + \sqrt{(2 + \sqrt{3})^2}$
 $= 2 - \sqrt{3} + 2 + \sqrt{3} = 4$

Lallu: $\sqrt{\sqrt{3}^2 + 2^2 - 2 \cdot 2 \cdot \sqrt{3}} + \sqrt{\sqrt{3}^2 + 2^2 + 2 \cdot 2 \cdot \sqrt{3}}$
 $\sqrt{(\sqrt{3} - 2)^2} + \sqrt{(\sqrt{3} + 2)^2}$
 $= \sqrt{3} - 2 + \sqrt{3} + 2$
 $= 2\sqrt{3}$

Dono galat

Tillu: $\sqrt{\sqrt{3}^2 + 2^2 - 2 \cdot 2 \cdot \sqrt{3}} + \sqrt{\sqrt{3}^2 + 2^2 + 2 \cdot 2 \cdot \sqrt{3}}$
 $\sqrt{(\sqrt{3} - 2)^2} + \sqrt{(\sqrt{3} + 2)^2}$
 $= |\sqrt{3} - 2| + |\sqrt{3} + 2|$
 $\quad \quad \quad \text{---ve} \quad \quad \quad \text{+ve}$
 $= -(\sqrt{3} - 2) + \sqrt{3} + 2$
 $= 4$

QUESTION



$$\frac{2}{\sqrt{2}} = \frac{\sqrt{2} \times \sqrt{2}}{\sqrt{2}} = \sqrt{2}$$

Let $n = \sqrt{6 + \sqrt{11}} + \sqrt{6 - \sqrt{11}} - \sqrt{22}$, then

A $n \geq 1$

B $0 < n < 1$

C $n = 0$

D $-1 < n < 0$

$$n = \sqrt{6 + \sqrt{11}} + \sqrt{6 - \sqrt{11}} - \sqrt{22}$$

$$n = \frac{\sqrt{2} \cdot \sqrt{6 + \sqrt{11}}}{\sqrt{2}} + \frac{\sqrt{2} \cdot \sqrt{6 - \sqrt{11}}}{\sqrt{2}} - \sqrt{22}$$

$$= \frac{\sqrt{12 + 2\sqrt{11}} + \sqrt{12 - 2\sqrt{11}}}{\sqrt{2}} - \sqrt{22}$$

$$= \frac{\sqrt{\sqrt{11}^2 + 1^2 + 2 \cdot \sqrt{11} \cdot 1} + \sqrt{\sqrt{11}^2 + 1^2 - 2\sqrt{11}}}{\sqrt{2}} - \sqrt{22}$$

$$= \frac{\overset{+ve}{\sqrt{11} + 1} + \overset{+ve}{\sqrt{11} - 1}}{\sqrt{2}} - \sqrt{22} = \frac{\sqrt{11} + 1 + \sqrt{11} - 1}{\sqrt{2}} - \sqrt{22} \rightarrow n = 0$$

$$= \frac{2\sqrt{11}}{\sqrt{2}} - \sqrt{22} = \sqrt{2} \times \sqrt{11} - \sqrt{22} = \sqrt{22} - \sqrt{22}$$

QUESTION



Tahoi

If $x = \sqrt{33 - 20\sqrt{2}}$ & $y = \sqrt{54 - 20\sqrt{2}}$ then value of $x - y$ is equal to

- A** $3(1 + \sqrt{2})$
- B** $7(\sqrt{2} - 1)$
- C** $\frac{-7}{1 + \sqrt{2}}$
- D** $7(1 + \sqrt{2})$

Ans. C

QUESTION



Tah 02

If $S_n = \frac{1}{\sqrt{1} + \sqrt{4}} + \frac{1}{\sqrt{4} + \sqrt{7}} + \frac{1}{\sqrt{7} + \sqrt{10}} + \dots$ n terms then -

- A** $S_8 = \frac{4}{3}$
- B** $S_{16} = 2$
- C** $S_{33} = 3$
- D** $S_{40} = \frac{10}{3}$

QUESTION



Let $0 < x < 1$ then $\sqrt{(x-1)^2} + \sqrt[4]{(2x+1)^4} - \sqrt[3]{\left(x-\frac{1}{2}\right)^3}$ is equal to

~~A~~ $\frac{5}{2}$

B $\frac{1}{2}$

C $-\frac{1}{2}$

D dependent of x

let $V = \underbrace{|x-1|}_{-ve} + \underbrace{|2x+1|}_{+ve} - \underbrace{\left(x-\frac{1}{2}\right)}_{+ve}$

Now $0 < x < 1 \Rightarrow x-1 = -ve$

$0 < x < 1 \Rightarrow 0 < 2x < 2 \Rightarrow 2x+1 = +ve$

~~$V = -(x-1) + 2x+1 - x + \frac{1}{2}$~~
 ~~$V = \frac{5}{2}$~~

Ans. A

QUESTION



Tah03

If $x = \sqrt{2 + \sqrt{3}} + \sqrt{4 - \sqrt{15}}$ then value of $\sqrt{2}x$ is equal to

- A** $\sqrt{5} - \sqrt{3}$
- B** $\sqrt{5} - 1$
- C** $\sqrt{3} + \sqrt{5}$
- D** $\sqrt{5} + 1$

Ans. D

QUESTION



Let $x = \sqrt[3]{2 + \sqrt{5}} + \sqrt[3]{2 - \sqrt{5}}$, then $x^3 + 3x$ is equal to

A 1

B 2

C 3

D 4

CBS

$$x^3 = \cancel{2} + \cancel{\sqrt{5}} + \cancel{2} - \cancel{\sqrt{5}} + 3 \cdot \sqrt[3]{2 + \sqrt{5}} \cdot \sqrt[3]{2 - \sqrt{5}} \left(\underbrace{\sqrt[3]{2 + \sqrt{5}} + \sqrt[3]{2 - \sqrt{5}}}_x \right)$$

$$x^3 = 4 + 3 \cdot \sqrt[3]{4 - 5} \cdot x$$

$$x^3 = 4 + 3 \sqrt[3]{-1} \cdot x = 4 - 3x$$

$$x^3 + 3x = 4$$

Ans. D

QUESTION

Tahoy

If $a = \sqrt{6 + 2\sqrt{5}} - \sqrt{6 - 2\sqrt{5}}$; $b = \sqrt[3]{6\sqrt{3} + 10} + \sqrt[3]{10 - 6\sqrt{3}}$, then the value of (ab) is equal to

A 8

B 12

C 4

D 6

QUESTION

If $|x^2 - 1| + (x - 1)^2 + \sqrt{x^2 - 3x + 2} = 0$, then value of x is :

~~A~~ 1

B 4

C -2

D None of these

$$|x^2 - 1| = 0 \quad \text{---} \quad x^2 - 1 = 0 \Rightarrow x = \pm 1$$

$$(x - 1) = 0 \Rightarrow x = 1$$

$$x^2 - 3x + 2 = 0 \Rightarrow x = 1, 2$$

$$x = 1$$

QUESTION



The number of real solutions of the equation $(x-1)^4 + (x-2)^4 + (x-3)^4 = 0$, is

$$\geq 0 \quad \geq 0 \quad \geq 0$$

A 4

B 2

C 1

~~**D**~~ 0

$$\begin{array}{l} (x-1)^4 = 0 \quad \text{---} \quad x=1 \\ \& (x-2)^4 = 0 \quad \text{---} \quad x=2 \\ \& (x-3)^4 = 0 \quad \text{---} \quad x=3 \end{array} \quad \cap \quad x \in \phi$$

QUESTION



Find the number of solutions for the equation $|x - 3|^2 + |x - 4| + x^2 + 7 = 0$.



Ashish Sir's Novel Concepts (ASNC)



Simon's Factoring Technique

$$\begin{aligned}\textcircled{1} \quad pq - p - q &= p(q-1) - q + 1 - 1 \\ &= p(q-1) - 1(q-1) - 1 \\ &= (p-1)(q-1) - 1\end{aligned}$$

$$\begin{aligned}\textcircled{2} \quad \underbrace{pq + p + q} &= p(q+1) + q + 1 - 1 \\ &= p(q+1) + 1 \cdot (q+1) - 1 \\ &= (p+1)(q+1) - 1\end{aligned}$$

If $m, n \in \mathbb{N}$ then find the number of ordered pairs (m, n) such that $\frac{2}{m} + \frac{2}{n} = 1$.

M①

Ans: 3 ordered pairs

$$\frac{2}{m} + \frac{2}{n} = 1$$

$$\frac{2n + 2m}{mn} = 1$$

$$2m + 2n = mn$$

$$2m + 2n - mn = 0$$

$$2m - n(m-2) = 0$$

$$2m - 4 + 4 - n(m-2) = 0$$

$$2(m-2) - n(m-2) + 4 = 0$$

$$(2-n)(m-2) = -4$$

$$-(n-2)(m-2) = -4$$

$$(m-2)(n-2) = 4$$

$m-2$	$n-2$	(m, n)
1	4	$(3, 6)$ ✓
4	1	$(6, 3)$ ✓
2	2	$(4, 4)$ ✓
-4	-1	$(-2, 1)$
-1	-4	$(1, -2)$
-2	-2	$(0, 0)$

If $m, n \in \mathbb{N}$ then find the number of ordered pairs (m, n) such that $\frac{2}{m} + \frac{2}{n} = 1$.

M(2)

$$\frac{2}{m} + \frac{2}{n} = 1$$

$$\frac{2n + 2m}{mn} = 1$$

$$2m + 2n = mn$$

$$2n = mn - 2m$$

$$2n = m(n-2)$$

$$m = \frac{2n}{n-2} = \frac{2n-4+4}{n-2} = \frac{2(n-2)}{n-2} + \frac{4}{n-2}$$

$$m = 2 + \frac{4}{n-2}$$



$$m = 2 + \frac{4}{n-2}$$

$n-2$ should be a divisor of 4

$$n-2 = -1, -2, -4, 1, 2, 4$$

$$\begin{array}{ccccccc}
 n = & 1 & , & 0 & , & -2 & , & 3 & , & 4 & , & 6 \\
 & & & \swarrow & & \searrow & & \downarrow & & \downarrow & & \downarrow \\
 m = & -2 & , & - & , & - & , & 6 & & 4 & & 3
 \end{array}$$

$$(m, n) = (6, 3), (3, 6), (4, 4)$$

QUESTION



Tan05

If x & y are positive integers, such that $\frac{1}{x} + \frac{1}{y} = \frac{1}{6}$ & $x \geq y$, then the number of ordered pairs of (x, y) is



Polynomials



An algebraic expression of the form

$$p(x) = a_n x^n + a_{n-1} x^{n-1} + a_{n-2} x^{n-2} + \dots + a_1 x^1 + a_0 x^0, \text{ where}$$

(i) $a_n \neq 0$

(ii) power of x is whole number, is called a polynomial in one variable.

$\nexists x: p(x) = x^3 - 6x^2 + \frac{7}{x} - 3$ \times $7 \cdot x^{-1}$
 $\nexists x: p(x) = x^6 - 6x^5 - 4x^3 + 7x + \sqrt{x}$ \times $x^{\frac{1}{2}}$

$a_n = \text{leading coeff}$
 $a_0 = \text{constant term / absolute term.}$

Hence, $a_n, a_{n-1}, a_{n-2}, \dots, a_0$ are coefficients of x^n, x^{n-1}, \dots, x^0 respectively and $a_n x^n, a_{n-1} x^{n-1}, a_{n-2} x^{n-2}, \dots$ are terms of the polynomial. Here the term $a_n x^n$ is called the **Leading term** and its coefficient a_n , the leading coefficient.

If leading coefficient is '1' then the polynomial is called as **monic polynomial**.

Ex: $P(x) = x^7 - 4x^3 + 3x + \pi$

- Yes a polynomial
- $7 = \text{degree}$
- leading coeff = 1
- absolute term = π
- Yes also a monic poly.



Degree of Polynomial

Degree of the polynomial in one variable is the largest exponent of the variable.

For example, the degree of the polynomial $3x^7 - 4x^6 + x + 9$ is 7 and the degree of the polynomial $5x^6 - 4x^2 - 6$ is 6.



Degree of Polynomial



$$0 \cdot x^7, 0 \cdot x^3, 0x^{10}$$

Polynomials classified by degree

Degree	Name	General form	Example
(undefined)	Zero polynomial	0	0
0	(Non-zero) constant polynomial	$a; (a \neq 0)$	1
1	Linear polynomial	$ax + b; (a \neq 0)$	$x + 1$
2	Quadratic polynomial	$ax^2 + bx + c; (a \neq 0)$	$x^2 + 1$
3	Cubic polynomial	$ax^3 + bx^2 + cx + d; (a \neq 0)$	$x^3 + 1$

Usually, a polynomial of degree n , for n greater than 3, is called a polynomial of degree n , although the phrases quadratic polynomial and quintic polynomial are sometimes used.



Remainder & Factor Theorem



Remainder Theorem

Let $P(x)$ be a polynomial of degree ≥ 1 and 'a' is any real number. If $P(x)$ is divided by $(x - a)$, then the remainder is $P(a)$.

Ex: find remainder when

$P(x) = x^4 - x^3 + 3x^2 - 2x + 1$ is divided by

a) $x - 1 \rightarrow \text{Rem} = P(1) = 1 - 1 + 3 - 2 + 1 = 2$

b) $x + 1 \rightarrow \text{Rem} = P(-1) = 1 + 1 + 3 + 2 + 1 = 8$

Factor Theorem

Let $P(x)$ be a polynomial of degree ≥ 1 and 'a' be any real constant such that $P(a) = 0$, then $(x - a)$ is a factor of $P(x)$. Conversely, if $(x - a)$ is a factor of $P(x)$, then $P(a) = 0$.

Divisor

$$x + a$$

$$x - a$$

$$ax + b$$

Rem

$$P(-a)$$

$$P(a)$$

$$P(-b/a)$$

$$\begin{array}{r}
 \text{Quotient} \\
 Q(x) \\
 x-a \overline{) P(x)} \text{--- dividend} \\
 \underline{} \\
 r(x) \text{--- Rem.}
 \end{array}$$

divisor

proof: $P(x) = (x-a)Q(x) + \text{Rem}$

put $x=a$

$$P(a) = 0 \cdot Q(a) + \text{Rem}$$

$$P(a) = \text{Remainder}$$

Remainder
Theorem

Dividend = Quotient \times Divisor + Rem

degree Rem < degree of divisor

Factor Thm

If Rem = 0 i.e. $P(a) = 0$

\Downarrow
 $(x-a)$ is a factor.
of $P(x)$

Note:

Let $P(x)$ be any polynomial of degree greater than or equal to one. If leading coefficient of $P(x)$ is 1 then $P(x)$ is called monic. (Leading coefficients means coefficients of highest power.)

**Don't Forget to
Retry all the class illustrations**



Today's KTK



No Selection $\xrightarrow{\text{TRISHUL Apnao IIT Jao}}$ **Selection with Good Rank**



The expression $\sqrt{12 + 6\sqrt{3}} + \sqrt{12 - 6\sqrt{3}}$ simplifies to

- A** 4
- B** $2\sqrt{3}$
- C** $3\sqrt{3}$
- D** 6



Let p, q be real numbers satisfying $p^2 - q^2 = 4$ and $2pq = 3$ then $(p^2 + q^2)$ is equal to

- A** 1
- B** 9
- C** 16
- D** 5

Value of x satisfying the equation $\sqrt{x^2 + 2x - 63} + |x^2 - 9x + 14| = 0$ is

The expression $\sqrt{28 + 10\sqrt{3}} + \sqrt{28 - 10\sqrt{3}}$ simplifies to

- A** 10
- B** 12
- C** $2\sqrt{3}$
- D** 5

Find all the integral solutions of the equation $xy = 2x - y$.

Ans. $(0, 0), (-2, 4), (1, 1), (-3, 3)$

Solution to Previous TAH

QUESTION



If a, b, c are distinct real numbers such that $a^2 - b = b^2 - c = c^2 - a$, then
 $(a + b)(b + c)(c + a) =$ _____

Piyush Bhadohi UP



TAH 01

Given: $a^2 - b = b^2 - c = c^2 - a$

We have,

$$\Downarrow$$
$$a^2 - b = b^2 - c$$

$$a^2 - b^2 = b - c$$

$$(a+b)(a-b) = b-c \Rightarrow a+b = \frac{b-c}{a-b}$$

lly, $b+c = \frac{c-a}{b-c}$ and $a+c = \frac{b-a}{a-c}$

$$\text{Now, } (a+b)(b+c)(c+a) = \frac{(b-c)(c-a)(b-a)}{(b-c)(a-b)(a-c)} = 1 \quad \checkmark$$

Q-1! If a, b, c are distinct real numbers such
TAH-1 that $a^2 - b = b^2 - c = c^2 - a$, then
 $(a+b)(b+c)(c+a) = ?$

Soln

$$a^2 - b = b^2 - c = c^2 - a$$

$$a^2 - b = b^2 - c \Rightarrow a^2 - b^2 = b - c \Rightarrow (a-b)(a+b) = (b-c) \quad \text{--- (i)}$$

$$b^2 - c = c^2 - a \Rightarrow b^2 - c^2 = c - a \Rightarrow (b+c)(b-c) = (c-a) \quad \text{--- (ii)}$$

$$a^2 - b = c^2 - a \Rightarrow a^2 - c^2 = b - a \Rightarrow (a+c)(a-c) = (b-a) \quad \text{--- (iii)}$$

(i) \times (ii) \times (iii):

$$(a+b)(b+c)(c+a)(a-b)(b-c)(a-c) = (b-c)(c-a)(b-a)$$

$$\text{or, } (a+b)(b+c)(c+a) \cancel{(a-b)} \cancel{(b-c)} \cancel{(c-a)} \times \cancel{(b-a)} = \cancel{(b-c)} \cancel{(c-a)} \cancel{(a-b)} \times \cancel{(b-a)}$$

$$\text{or, } (a+b)(b+c)(c+a) = 1$$

$\therefore \text{Ans.} = 1$

$$\left[\begin{array}{l} \because a, b, c \text{ are distinct} \\ \Downarrow \\ a-b \neq b-c \neq c-a \\ \neq 0 \end{array} \right]$$

TAH 01

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QUESTION



If x , y & z are three real numbers such that $x^2 + 4y^2 + 9z^2 - 2x - 4y - 6z + 3 = 0$ then find the value of $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$.

* IRH-02:-

Solⁿ $x^2 + 4y^2 + 9z^2 - 2x - 4y - 6z + 3 = 0$
 \Downarrow $1+1+1$ (split)

$$\underbrace{x^2 - 2x + 1} + \underbrace{4y^2 - 4y + 1} + \underbrace{9z^2 - 6z + 1} = 0$$
$$(x-1)^2 + (2y-1)^2 + (3z-1)^2 = 0$$

$x-1=0$	$2y-1=0$	$3z-1=0$
$x=1$	$y=1/2$	$z=1/3$

find

$$\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = \frac{1}{1} + 2 + 3 = 6$$

2) Tah 02

If x, y & z are three real numbers such that
 $x^2 + 4y^2 + 9z^2 - 2x - 4y - 6z + 3 = 0$, then find
the value of $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$.

$$x^2 - 2x + 1 + 4y^2 - 4y + 1 + 9z^2 - 6z + 1 = 0$$

$$(x-1)^2 + (2y-1)^2 + (3z-1)^2 = 0$$

$$x-1 = 0$$

$$\underline{\underline{x=1}}$$

$$2y-1 = 0$$

$$2y = \frac{1}{2}$$

$$3z-1 = 0$$

$$z = \frac{1}{3}$$

$$\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = \frac{1}{1} + \frac{1}{1/2} + \frac{1}{1/3}$$

$$= 1 + 2 + 3$$

$$= 6 //$$

Q-2: If x, y, z are three real numbers such that $x^2 + 4y^2 + 9z^2 - 2x - 4y - 6z + 3 = 0$; then find the value of $\frac{1}{x} + \frac{1}{y} + \frac{1}{z}$.

Soln: $x^2 + 4y^2 + 9z^2 - 2x - 4y - 6z + 3 = 0$.

or, $x^2 - 2x + 4y^2 - 4y + 9z^2 - 6z + 3 = 0$.

or, $x^2 - 2 \cdot x \cdot 1 + 1^2 - 1^2 + (2y)^2 - 2 \cdot 2y \cdot 1 + 1^2 - 1^2 + (3z)^2 - 2 \cdot 3z \cdot 1 + 1^2 - 1^2 + 3 = 0$.

or, $(x-1)^2 - 1 + (2y-1)^2 - 1 + (3z-1)^2 - 1 + 3 = 0$.

or, $(x-1)^2 + (2y-1)^2 + (3z-1)^2 - 3 + 3 = 0$.

or, $(x-1)^2 + (2y-1)^2 + (3z-1)^2 = 0$.

$\therefore x=1 \quad \left\{ \begin{array}{l} 2y=1 \\ \text{or, } y=\frac{1}{2} \end{array} \right. \quad \left\{ \begin{array}{l} 3z=1 \\ \text{or, } z=\frac{1}{3} \end{array} \right.$

$\therefore \frac{1}{x} + \frac{1}{y} + \frac{1}{z}$
 $= \frac{1}{1} + \frac{1}{1/2} + \frac{1}{1/3}$
 $= 1 + 2 + 3$
 $= 6 \quad (\text{Ans.})$

TAH 02
 SAYANTAN MANNA
 WEST BENGAL

QUESTION



Let a, b, c are real numbers and satisfy $a = 8 - b$ and $c^2 = ab - 16$, then $\frac{a}{b}$ is equal to

TAH 3

$$(a+b)^2 = 8^2$$
$$a^2 + b^2 + 2ab = 64 \text{ --- (I)}$$

$$a = 8 - b$$

$$c^2 = ab - 16 \Rightarrow ab = c^2 + 16 \text{ --- (II)}$$

put ab in (I) eq

$$a^2 + b^2 + 2(c^2 + 16) = 64$$

$$\Rightarrow (a-b)^2 + 2ab + 2(c^2 + 16) = 64$$

$$\Rightarrow (a-b)^2 + 4c^2 + 64 = 64$$

$$\Rightarrow (a-b)^2 + 4c^2 = 0$$

$$\text{and } c = 0$$

$$\therefore a = b$$

$$\boxed{\frac{a}{b} = 1}$$

Ans.

Ash Man
Maity

3) Tak os

Let a, b, c are real numbers and satisfy
 $a = 8 - b$ and $c^2 = ab - 16$, then $\frac{a}{b}$ is equal to

$$c^2 = (8 - b)b - 16$$

$$c^2 = 8b - b^2 - 16$$

$$c^2 = -b^2 + 8b - 16$$

$$c^2 = -(b^2 - 8b + 16)$$

$$c^2 \in \mathbb{R}, c^2 \geq 0$$

$$-(b^2 - 8b + 16) \geq 0$$

$$b^2 - 8b + 16 \geq 0$$

$$(b - 4)(b - 4) \geq 0$$

$$(b - 4)^2 \geq 0$$

$$b - 4 = 0$$

$$\underline{\underline{b = 4}}$$

$$a = 8 - b$$

$$a = 8 - 4$$

$$= 4 //$$

$$\frac{a}{b} = \frac{4}{4} = 1 //$$

Solution to Previous KTKs

a, b, c are reals such that $a + b + c = 3$ and $\frac{1}{a+b} + \frac{1}{b+c} + \frac{1}{c+a} = \frac{10}{3}$.

The value $E = \frac{a}{b+c} + \frac{b}{c+a} + \frac{c}{a+b}$ is

- A** 9
- B** 7
- C** 5
- D** 3

(K.T.K-1) a, b, c are reals such that $a+b+c=3$
and $\frac{1}{a+b} + \frac{1}{b+c} + \frac{1}{c+a} = \frac{10}{3}$ Then value

$$x = \frac{a}{b+c} + \frac{b}{a+c} + \frac{c}{a+b} \text{ is}$$

Solⁿ $\rightarrow a+b+c=3 \text{ --- (i)}$ **Abhishek Kumar**

$$\frac{1}{a+b} + \frac{1}{b+c} + \frac{1}{c+a} = \frac{10}{3} \text{ --- (ii)}$$

eq (i) x (ii)

$$1 + \frac{c}{(a+b)} + 1 + \frac{a}{(b+c)} + 1 + \frac{b}{(a+c)} = 10$$

$$\frac{a}{(b+c)} + \frac{b}{(a+c)} + \frac{c}{(a+b)} = 10 - 3$$

$$= \textcircled{7}$$

15



Problem 3
a, b, c are reals such that $a+b+c=3$ and $\frac{1}{a+b} + \frac{1}{b+c} + \frac{1}{c+a} = \frac{10}{3}$, Find $E = \frac{a}{a+c} + \frac{b}{c+a} + \frac{c}{a+b}$

Solⁿ $E = \frac{a}{a+c} + \frac{b}{c+a} + \frac{c}{a+b}$

$\rightarrow \frac{1}{a+b} + \frac{1}{b+c} + \frac{1}{c+a} = \frac{10}{3}$ given

**Soumay
Pandey**

$\rightarrow \frac{a+b+c}{a+b} + \frac{a+b+c}{b+c} + \frac{a+b+c}{c+a} = 10$

$\rightarrow \left(\frac{a+b+c}{a+b} \right) + \left(\frac{a+b+c}{b+c} \right) + \left(\frac{a+b+c}{c+a} \right) = 10$
 $\{ \because a+b+c=3 \}$

$\rightarrow \left(1 + \frac{c}{a+b} \right) + \left(1 + \frac{a}{b+c} \right) + \left(1 + \frac{b}{c+a} \right) = 10$

Finally

$\frac{a}{b+c} + \frac{b}{c+a} + \frac{c}{a+b} = 10 - 3 = \textcircled{7} \text{ Ans}$

Solve the equations : $\begin{cases} 2^x + 3^y = 41 \\ 2^{x+2} + 3^{y+2} = 209 \end{cases}$

Ans. $x = 5$ and $y = 2$

Q-3:- Solve the equations!

$$\begin{cases} 2^x + 3^y = 41 \\ 2^{x+2} + 3^{y+2} = 209 \end{cases}$$

Soln:-

$$2^x + 3^y = 41 \quad \text{--- (i)}$$

$$2^{x+2} + 3^{y+2} = 209$$

$$\text{or } 2^x \times 4 + 3^y \times 9 = 209$$

$$\text{or } 4 \cdot 2^x + 9 \cdot 3^y = 209 \quad \text{--- (ii)}$$

$$\text{Let } 2^x = t, \quad 3^y = s.$$

$$t + s = 41 \quad \text{--- (i) } \times 4$$

$$4t + 9s = 209 \quad \text{--- (ii)}$$

$$4t + 4s = 164$$

$$4t + 9s = 209$$

(Subtract)

$$5s = 45$$

$$\text{or } \boxed{s = 9}$$

$$\text{or } 3^y = 9$$

$$\text{or } 3^y = 3^2$$

$$\text{or } \boxed{y = 2}$$

$$\therefore t = 41 - 9$$

$$\text{or } \boxed{t = 32}$$

$$\text{or } 2^x = 32$$

$$\text{or } 2^x = 2^5$$

$$\text{or } \boxed{x = 5}$$

$$\therefore \text{Ans.} \rightarrow x = 5, y = 2$$

KTK 2

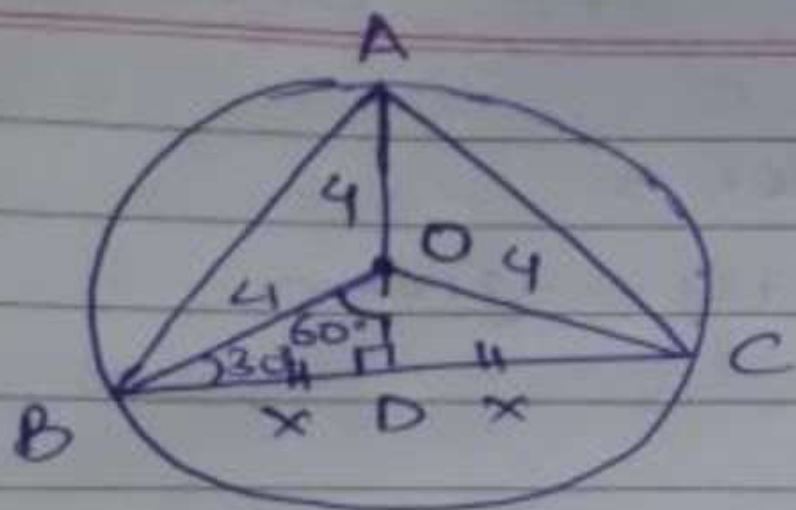
SAYANTAN MANNA

WEST BENGAL

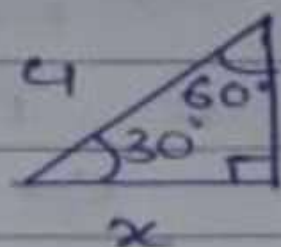
What is the area of an equilateral triangle inscribed in a circle of radius 4 cm?

- A** 12 cm^2
- B** $9\sqrt{3} \text{ cm}^2$
- C** $8\sqrt{3} \text{ cm}^2$
- D** $12\sqrt{3} \text{ cm}^2$

- What is the area of an equilateral triangle inscribed in circle of radius of 4cm?



In $\triangle OBD$,



$$\sin 60^\circ = \frac{P}{H} = \frac{x}{4}$$

$$\frac{\sqrt{3}}{2} = \frac{x}{4}$$

$$\boxed{x = 2\sqrt{3}}$$

Now

$$BC = 2x = 2(2\sqrt{3}) = 4\sqrt{3}$$

$$\text{Area of } \triangle ABC = \frac{\sqrt{3}}{4} a^2$$

$$= \frac{\sqrt{3}}{4} \cdot 4\sqrt{3} \cdot 4\sqrt{3}$$

$$= 12\sqrt{3} \text{ cm}^2$$

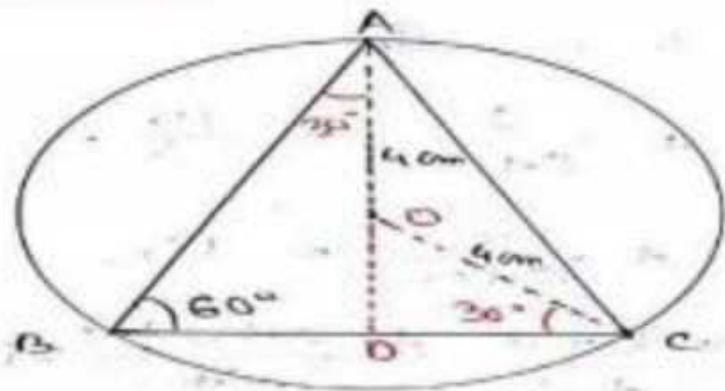
Richard Feynman
Jharkhand

- Q-2) What is the area of an equilateral triangle inscribed in a circle of radius 4 cm?

(A) 12 cm^2 (B) $9\sqrt{3} \text{ cm}^2$ (C) $8\sqrt{3} \text{ cm}^2$ (D) $12\sqrt{3} \text{ cm}^2$

Soln:

→ method-1:



KTK 03 PART 1
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In ΔCOD ,

$$\sin 30^\circ = \frac{OD}{OC}$$

$$\text{or, } \frac{1}{2} = \frac{OD}{4}$$

$$\text{or, } OD = 2 \text{ cm.}$$

Height of ΔABC

$$= AD$$

$$= AO + OD$$

$$= 4 + 2 = 6 \text{ cm.}$$

In ΔCOD ,

$$\cos 30^\circ = \frac{CD}{OC}$$

$$\text{or, } \frac{\sqrt{3}}{2} = \frac{CD}{4}$$

$$\text{or, } CD = 2\sqrt{3}$$

side of triangle

$$ABC = BC$$

$$= BD + CD$$

$$= 2 \times CD$$

$$= 2 \times 2\sqrt{3}$$

$$= 4\sqrt{3} \text{ cm.}$$

$$\therefore \text{Area} = \frac{1}{2} \times \text{Base} \times \text{Height}$$

$$= \frac{1}{2} \times 8 \times 4\sqrt{3}$$

$$= 12\sqrt{3} \text{ cm}^2.$$

$$\therefore \text{Ans.} \Rightarrow \text{(D) } 12\sqrt{3} \text{ cm}^2$$



Mann ki Baat

- Masum Gadhara ✓ (A) — 5.91%.
- Gadhara Jo khud ko Gadhara samajhtay ✓ (B) — 4.1%.
- Voh Gadhara jisay maloom hai (C) — 76%.
- Voh Gadhara. ✓ — selection.
- Ghodaar ✓ — selection (D) — 14%.

THANK
YOU